COMPONENT 2: CALCULATOR-ALLOWED MATHEMATICS. HIGHER TIER

GENERAL INSTRUCTIONS for MARKING GCSE Mathematics

1. The mark scheme should be applied precisely and no departure made from it. Marks should be awarded directly as indicated and no further subdivision made. When a candidate follows a method that does not correspond to the methods explicitly set out in the mark scheme, marks should be awarded in the spirit of the mark scheme. In such cases, further advice should be sought from the Team Leader or Principal Examiner.

2. Marking Abbreviations

The following may be used in marking schemes or in the marking of scripts to indicate reasons for the marks awarded.

CAO = correct answer only

MR = misread

PA = premature approximation

bod = benefit of doubt

oe = or equivalent

si = seen or implied

ISW = janore subsequent working



F.T. = follow through (\checkmark indicates correct working following an error and \checkmark indicates a further error has been made)

Anything given in brackets in the marking scheme is expected but, not required, to gain credit.

3. Premature Approximation

A candidate who approximates prematurely and then proceeds correctly to a final answer loses 1 mark as directed by the Principal Examiner.

4. Misreads

When the data of a question is misread in such a way as not to alter the aim or difficulty of a question, follow through the working and allot marks for the candidates' answers as on the scheme using the new data.

This is only applicable if a wrong value, is used consistently throughout a solution; if the correct value appears anywhere, the solution is not classed as MR (but may, of course, still earn other marks).

5. Marking codes

- 'M' marks are awarded for any correct method applied to appropriate working, • even though a numerical error may be involved. Once earned they cannot be lost.
- 'm' marks are dependent method marks. They are only given if the relevant previous 'M' mark has been earned.
- 'A' marks are given for a numerically correct stage, for a correct result or for an • answer lying within a specified range. They are only given if the relevant M/m mark has been earned either explicitly or by inference from the correct answer.
- 'B' marks are independent of method and are usually awarded for an accurate • result or statement.
- 'S' marks are awarded for strategy •
- 'E' marks are awarded for explanation •
- 'U' marks are awarded for units •
- 'P' marks are awarded for plotting points
- 'C' marks are awarded for drawing curves

COMPONENT 2: CALCULATOR-ALLOWED MATHEMATICS, HIGHER TIER

Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
1. (a) 28416/38400) × 100 74(%)	M1 A1	1.3a 1.3a	Or equivalent full method
(b) 766 + 766 × 12/100 OR 766 × 1.12	M1 A1	1.3a 1.3a	Or equivalent full method
	(4)	(4)AO1 (0)AO2 (0)AO3	
2. (a) Reason, e.g. 'outside the juice bar', 'mostly younger people use juice bars'	E1	2.5b	
(b) Two appropriate criticisms e.g. 'No under 15s', '30 appears in two boxes' 'may object to giving their age'	E2	2.5b	
boxes, may object to giving their age	(3)	(0) AO1 (3) AO2 (0) AO3	
3. $6x - 2 = 4x + 5$	B1	2.2	
2x = 7	B1	1.3a	
x = 7/2 (3.5)	B1	1.3a	
$4 \times 3.5 + 5$ or $6 \times 3.5 - 2$	M1	2.2	
=19 (cm)	A1	1.3a	
	(5)	(3) AO1 (2) AO2 (0) AO3	
4.(a) Reasonable straight line of best fit by eye, some points above and below	B1	1.3a	
(b) Suitable description of the relationship e.g. 'higher the number of visitors, higher the donations'	B1	2.1b	Accept 'positive correlation' but not just 'positive'
(c) Indicates Sunday (12, 100)	B1	2.3a	
(d) (i) Valid explanation e.g. "By using the line of best fit" or "By using the relationship shown in the graph"	E1	2.1a	
(ii) Valid explanation e.g "You can't say for definite how many donations the centre will receive on a particular day"	E1	2.5a	
particular day	(5)	(1) AO1 (4) AO2 (0) AO3	

Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
5. (a) $(x =) \frac{1}{4}$ or 0.25 or equivalent	B1	1.3a	Accept embedded answers in (a) and (b) Accept 3/12. Mark final answer
(b) $9x-4 = 7x + 14$ 2x = 18 or equivalent x = 9	B1 B1 B1	1.3b 1.3b 1.3b	FT until 2 nd error
	(4)	(4) AO1 (0) AO2 (0) AO3	
6.(a) 7 <i>n</i> −1	B2	1.3a	B1 for $7n \pm$ Allow change of letter
(b) <i>a</i> + <i>a</i> +7+ <i>a</i> +14+ <i>a</i> +21=6 or equivalent <i>a</i> = −9 or lowest number = −9	M1 A1	3.1a 1.3a	
-9, -2, 5, 12	B1	1.3a	OR sight of at least 3 trials keeping to either difference criterion or sum criterion
	(5)	(4) AO1 (0) AO2 (1) AO3	
7. (Height of tree =) Tan 56° \times 19 + 1·8(m)	М3	3.1d	Award M2 for tan $56^{\circ} \times 19$ OR sight of $28 \cdot 168658(m)$ Award M1 for tan 56° = opposite/19 Accept rounded or truncated from working
(Height of tree =) 29·968658 (m)	A1	1.3b	Accept rounded or truncated from working F.T from their rounded or truncated 28:168
	(4)	(1) AO1 (0) AO2 (3) AO3	20 100
8.(a) Midpoints 52, 56, 60 and 64 52×12 + 56×32 + 60×14 + 64×2 (=3384)	B1 M1	1.3b 1.3b	F.T. their midpoints, provided within interval
/60	m1	1.3b	
56.4 (cm)	A1	1.3b	F.T. their sum of products, division by 60
(b) Strategy to look back that 32 out of 60 are size 2, e.g. '(table shows) about half customers are size 2	S1	2.5a	
Conclusion to give Salesman is correct	E1	2.5a	
	(6)	(4) AO1 (2) AO2 (0) AO3	

Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
9.(a) 8 (mm)	B1	2.3a	
(b) (i) Method e.g. increase in <i>L</i> / increase in <i>M</i>	M1	1.3a	Or idea of alternative complete method Accept sight of quotient based on misread of the scale for M1 only.
e.g. 12/150 (= 0.08)	A1	1.3a	Mark final answer.
(ii) Full explanation, e.g. 'rate of change of length with mass', 'for every 1 g increase 0.08 mm increase'	E1	2.3a	
(c) Plausible explanation, e.g. 'no more data recorded', 'spring snaps', 'broken spring', 'spring now completely straight', etc	E1	2.3a	
	(5)	(2) AO1 (3) AO2 (0) AO3	
10. Straight lines parallel to all 4 sides and 3cm away (<u>+</u> 2mm)	B2	2.3b	B1 for straight lines parallel to 2 sides and 3cm away (<u>+</u> 2mm), OR straight lines parallel to all 4 sides but not at 3cm
Arcs with radius 3cm (<u>+</u> 2mm) at all 4 vertices joining the straight lines	B2	2.3b	B1 for arcs with radius 3cm (<u>+</u> 2mm) at least 2 vertices but not joined to straight lines, OR arcs at all 4 vertices but not at 3cm or not joined to straight lines
	(4)	(0) AO1 (4) AO2 (0) AO3	not joined to straight lines
11. (a) $x + 3x + 16x = 1$	M1	1.1	Use of 'total probability = 1'
x = 1/20 or 0.05 or equivalent ISW	A1	1.3a	Accept 5% only if specified as a
(b) (Statement that Stephen is incorrect and) a correct explanation e.g. fraction (proportion) of tickets bought would be the same.	E1	2.5a	Accept alternative explanations such as 'It may decrease his chance of winning a prize as more people may be tempted to buy tickets'
	(3)	(2) AO1 (1) AO2 (0) AO3	

Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
12.(a) All three stages of the appropriate calculation $560 \times (4.55 \div 37.8) \times 1.48$	M3	3.1d	M2 for sight of $560 \times 455 \div 37.8$, OR M1 for sight of $560 \div 37.8$, $4.55 \div 37.8$, $37.8 \div 4.55$, or 4.55×1.48
			Note: $560 \div 37.8 (= 14.814814 \text{ gallons})$ $\times 4.55 (= 67.407 \text{ litres})$ Use of 14.8 gives 67.34, use of 15 gives 68.25
(£)99.76	A2	1.3a	Depends on M3 A1 for (£)99.7629 or 99.6632 or 101.01 or other amount from premature approximation
(b) 560 / 10·75 or 560 / 10 ¾	M2	3.1d	M1 for 560/10·45 or 560/675 or 560/645
52(·093 mph)	A1	1.3a	C.A.O
C selected or implied with a reason,	E1	2.1b	Only F.T. provided
travels fast'	(9)	(3) AO1 (1) AO2 (5) AO3	SU ≤ their average speed ≤ 70
13.(a) $2.3 \times 10^{30} / 2^5$ or equivalent	M2	3.1c	M1 for an attempt to divide 2.3×10^{30} by 2 more than once
7·2 ×10 ²⁸	A1	1.2	
(b) $r = 0.75^t \times x$	B3	2.3a	B2 for correct expression $0.75^t \times x$ B1 for $0.75x$, $x - 1/4x$, 0.75^2x , SC2 for $r = 0.25^t \times x$ or SC1 for $0.25^t \times x$ or equivalent
	(6)	(1) AO1 (3) AO2 (2) AO3	or equivalent
14 (a) 45 / 120 (×100) 37·5(%) rounded or truncated	M1 A1	1.3b 1.3b	Accept values from 44 to 46 inclusive leading to 36.66 to 38.33(%) rounded or truncated.
(b) 70 seconds means ≈ 100 × 85/120 OR 80% calls means (0:8 × 120 –) 96 calls	M1	3.1c	(OR 100 × $84/120 = 70\%$). 70 seconds gives 84 to 86 inclusive so
70·833% OR 71% OR ≈75 seconds AND interpretation 'No' (target not met stated or implied)	A1	2.1b	Alternative solution to (b): 'You can't tell', with full supported working for reasoning, gains M1 A1. e.g. percentage of calls answered in 70 seconds could be anything between
Stating an assumption made e.g. " assumed that the times between 60 and 80 are evenly distributed"	E1	3.4a	50% and 91.6666% Assumption: e.g. 'you don't know how the calls are distributed in the 60-80 group' gains E1.
	(5)	(2) AO1 (1) AO2 (2) AO3	

Specimen Assessment Materials		Elements	•
Calculator-allowed Higher	Mark	linked to	Comments
15 Use of A · B is 2 · 3 or sight of 2/5	B1	3 1a	
Area circle – $\pi \times 1.5^2$	B1	11	
$\Delta rea \Delta = (2/5) \times \pi \times 1.5^2$	M1	3.2	
$-2.8(27 \text{ cm}^2)$	A1	1.3a	
- 2 0(27 Chi)			
	(4)	(2) AO1 (0) AO2 (2) AO3	
16. $x = \left[-3 \pm \sqrt{(3^2 - (4 \times 2) - 3)} \right] / (2 \times 2)$	M1	1.3a	Allow one slip
$=\left[-3\pm\sqrt{33}\right]/4$	A1	1.3a	
0.69 and -2.19	A1	1.3a	CAO. Must be correct to 2 decimal places
	(3)	(3) AO1 (0) AO2 (0) AO3	
17. (a) Sight of 305(cm) or 3.05(m) AND 3.95(cm) or 0.0395(m)	B1	3.1d	The B1 may be awarded if these values are seen in (a) or in (b) and need not be of the same units
<u>305</u> or <u>3.05</u> 3.95 0.0395	M1	3.1d	F.T. 'their 305', provided it is > 300 and \leq 310 AND 'their 3.95', provided it is \geq 3 and < 4
= 77	A1	1.3a	77·2 is A0.
(b) (If container has height=) 295(cm) or 2·95(m) AND (each metal plate has thickness=) 4·05(cm) or 0·0405(m)	B1	2.4a	The B1 may be awarded if these values are seen in (a) or in (b) and need not be of the same units.
<u>295</u> or <u>2∙95</u> 4∙05 0∙0405	M1	2.4a	F.T. 'their 295', provided it is \geq 290 and < 300 AND 'their 4.05', provided it is > 4 and < 5
= 72.8	A1	2.4a	
			Alternative methods:
			73 × 4·05 M1
			= 295·6(5) AND 'this is >295' A1
			OR
			295/73 M1
		(1)	= 4.04 AND 'this is less than 4.05 ' A1
	(6)	(1) AO1	
		(3) AO2	
		(2) AO3	

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Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
18. (a) $(x =) 35^{\circ}$ Angles in same segment, (angles in triangle)	B1 E1	2.3a 2.3a	Dependent on B1, unless correct workings seen but with 1 error in their calculation Accept, e.g. 'angles from same chord'
(b) 40° Angle at the centre is twice the angle at circumference	B1 E1	2.3a 2.3a	Dependent on B1, unless correct workings seen but with 1 error in their calculation
(c) Angle $CAB = x$ AND stating alternate	B1	2.4b	May be indicated on the diagram
Stating triangle CAB isosceles AND $(180 - x)/2$	B1 (6)	2.4b (0) AO1 (6) AO2 (0) AO3	
19. Radius of the cylinder = 0.5 cm OR	B1	3.1d	Maybe shown on the diagram
Idea height of cylinder approximately circumference of ring	S1	3.1d	Maybe internal, external or somewhere in between. Accept sight of $8 \times \pi$ or $9 \times \pi$ for S1
Ring C = $2 \times \pi \times$ value between 8 and 9 inclusive	M1	3.1d	
Volume = $\pi \times 0.5^2 \times \text{ ring C}$	M1	3.1d	
Volume in the range 39.5 to 44.4 (cm ³)	A1	1.3a	C.A.O. E.g. 41.95 (cm ³) from use of 8.5
Statement about assumption, e.g. volume of cylinder used to calculate volume of dog toy, use of mid value for radius.	E1 F1	3.5 3.4a	Accept 'circumference of the ring is the same as the length of plastic', 'radius doesn't change as bend around' Do not accept 'radius is 0.5'
used smaller radius so volume will be greater, or used larger radius so volume will be less, or used 8.5 cm as height of cylinder is clearly between 8 cm and 9 cm		0.10	
	(7)	(1) AO1 (0) AO2 (6) AO3	
20.(a) Sight of $h \propto u^2$ or $h = ku^2$	B1	3.1d	May be implied in later working
$5 = k \times 10^2$	M1	3.1d	F.T. non-linear only in all parts
k = 0.05	A1	1.3a	Or equivalent. Ignore incorrect use of ∞ . NOTE: working for finding <i>k</i> (first three marks) may be seen in (b) not (a). Award the marks in (a) if this is the case
$h = 0.05 \times 12^2$	M1	3.1d	F.T. 'their k '
h = 7.2 (m) or equivalent	A1	1.3a	
(b) $16 / 0.05 = u^2$ (=320)	M1	1.3a	
u = 17·88854… (m/s)	A1 (7)	1.3a (4) AO1 (0) AO2 (3) AO3	Accept rounded or truncated

Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
21. Use of scale factor 1.5 or 2/3 as appropriate, or angles in ABC correctly as (60,) 80 and 40	M1	3.1b	
DE/sin 60 = 9/sin 40 or AB/sin60 = 6/sin40	M1	3.2	
$DE = 9 \times \sin 60/\sin 40$ or AB = 6 \times \sin 60/\sin 40	m1	1.3a	DE = 12(·126 cm)
AB = 8(·084 cm) or 8.1(cm)	A1	1.3a	
	(4)	(2) AO1 (0) AO2 (2) AO3	C.A.O. Alternative: M1 CD/sin80 = 9/sin40 or CD = sin80×9/sin40 OR AC/sin80 = 6/sin40 or AC = sin80×6/sin40 M1 AC = $\frac{2}{3}$ CD or AC =9.19 (CD=13·79) m1 AB ² = 6 ² + AC ² - 2×6×AC×cos60 (F.T. their AC but not their CD used) A1 AB = 8(·084cm) or 8·1(cm) C.A.O.
22.(a) Reasonable tangent drawn	S1	2.3a	With or without tongont
Calculated gradient for their tangent Units given m/s^2 or ms^{-2}	A1 U1	1.3a 1.1	(Answers may be in the range 25 to 37) Independent of other marks
(b) Attempt to find area by splitting up.	S1	3.1c	
Suitable area sections with at least 2 correct areas.	M2	3.1c	M1 Suitable area sections with at least 1 correct area. Allow tolerance in reading the velocity, as estimation required. Units not required
Answers in the range 134 (m) to 158 (m) from correct working	A1	1.3a	
(c) Appropriate improvement suggested e.g. "working with more trapeziums of narrower widths"	E1	3.4a	
	(9)	(4) AO1 (1) AO2 (4) AO3	

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Specimen Assessment Materials Calculator-allowed Higher	Mark	Elements linked to AOs	Comments
23. (a) $f(4) = 8$	B1	1.3a	
gf(4) = 19	B1	1.3a	F.I 'their f(4)'
			ef(x) = 3 + 2(2x) OR 3 + 4x B1
			gf(4) = 19 B1
(b) $fg(x) = 2(3 + 2x)$	M1	3.1b	
fg(x) = 6 + 4x	A1	1.3a	
6 + 4x = 14	M1	3.1b	Allow F.T. from 'their $6 + 4x$ ', provided it
<i>x</i> = 2	A1	1.3a	Is a linear expression, for M1 only C.A.O.
			<u>Alternative method</u> :
			fg(x) = 2(3+2x) M1 2(2+2x) = 14 M1
			2(3+2x) = 14 WI 3+2x-7 A1 C A O
			or equivalent without brackets
			x = 2 A1 C.A.O.
	(6)	(4) AO1	
		(0) AO2	
		(2) AO3	

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