AQA

GCSE
Mathematics
Specification (8300/3F)
Paper 3 Foundation tier

F

| Date | Morning | 1 hour 30 minutes |

Model Solutions

Materials

For this paper you must have:
- a calculator
- mathematical instruments.

Instructions
- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the bottom of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book.
- In all calculations, show clearly how you work out your answer.

Information
- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Please write clearly, in block capitals, to allow character computer recognition.

Centre number ☐☐☐☐☐ Candidate number ☐☐☐☐

Surname ☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐

Forename(s) ☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐☐

Candidate signature _____

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Answer **all** questions in the spaces provided.

1 Here are seven numbers.

13   6   12   7   6   4   8

13 − 4 = 9

1 (a) Work out the range of the seven numbers.

Circle your answer.

[1 mark]

5   6   7   8   (9)

1 (b) What is the mode of the seven numbers?
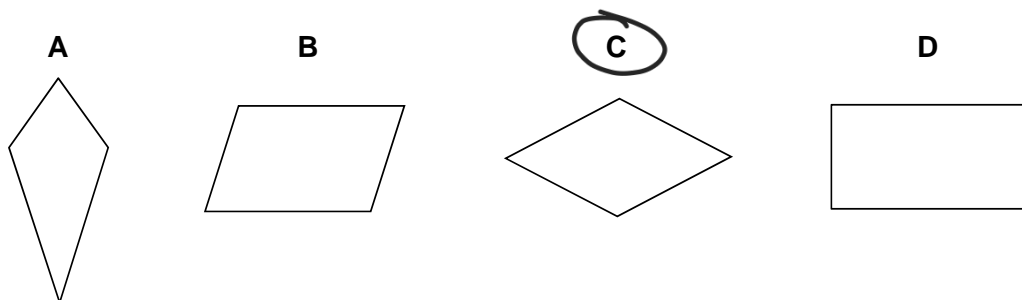
Circle your answer.

[1 mark]

5   (6)   7   8   9

because it appears the most

2 Which shape has **two** lines of symmetry **and** its diagonals intersecting at 90˚?

Circle the correct letter.

[1 mark]

A   B   **C**   D

3 Which of these is a cube number?

Circle your answer.

[1 mark]

3   9   27   100

$3 \times 3 \times 3 = 27$

Turn over for the next question

4   Liz buys a car for £7500

      She pays a deposit of £1875

      She pays the rest in 36 equal monthly payments.

Work out the amount of each monthly payment.

[3 marks]

£7500 − £1875 = £5625 to pay over 36 months

$$\frac{£5625}{36} = £156.25$$

Answer £ _____ 156.25 _____

5   120 men and 80 women were asked if they drive to work.

      Altogether $\frac{1}{4}$ of the people said yes.

      $\frac{1}{3}$ of the men said yes.

What fraction of the women said yes?

[4 marks]

120 + 80 = 200 total

1/4 of 200 said yes → 1/4 × 200 = 50 total 'yes'

1/3 men of 120 said yes → 1/3 × 120 = 40 men 'yes'

50 − 40 = 10 women 'yes'

10/80 = $\frac{1}{8}$ women 'yes'

Answer _____ 1/8 _____

6   Boxes A, B, C and D contain balls with numbers on them.

| Box A | Box B | Box C | Box D |
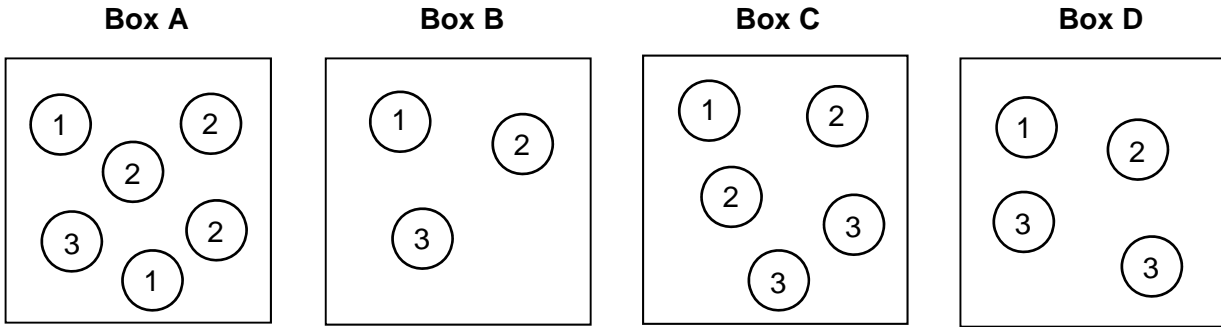
A ball is picked at random from each box.

6   (a)   Which box gives the **greatest** chance of picking a 3?

You **must** show your working.

[2 marks]

$A = 1/6 = 17.\bar{1}$

$B = 1/3 = 33.\bar{1}$

$C = 2/5 = 40\%$

$D = 2/4 = 1/2 = 50\%$

Box _____D_____

6   (b)   Which two boxes give the **same** chance of picking a 1?

[1 mark]

$A = 2/6 = 1/3$

$B = 1/3$

$C = 1/4$

Box _____A_____   and   Box _____B_____

7   Zayn records his weekly sales.
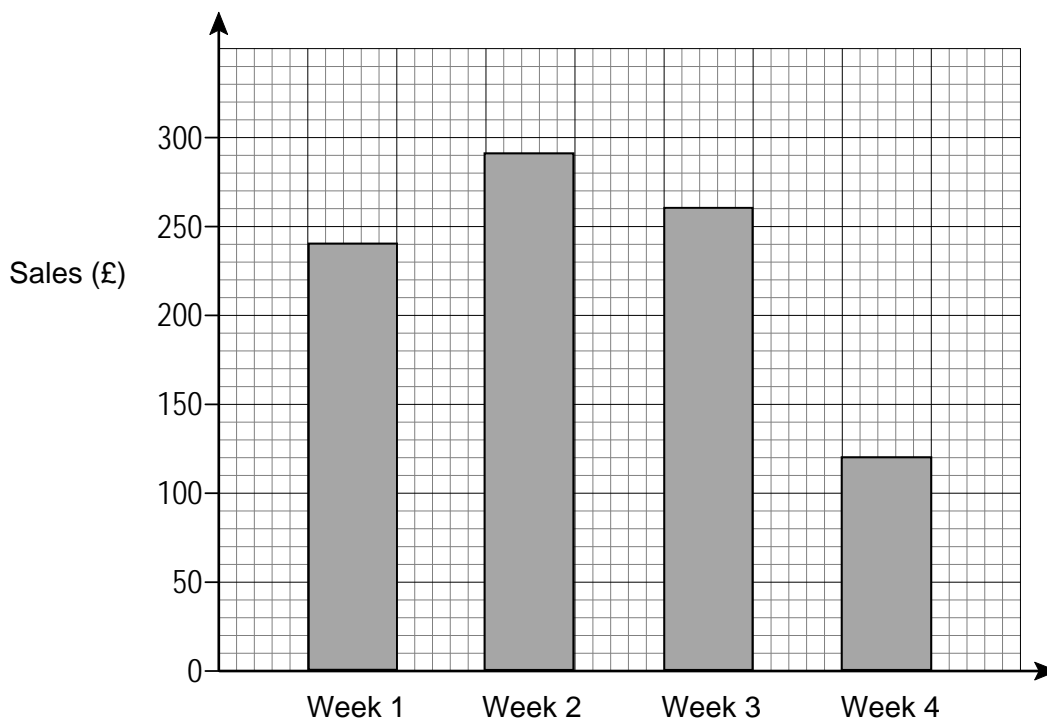
Every week his costs are £87.50

7 **(a)**   Work out his profit in Week 1

[2 marks]

$$240 - 87.50 = £152.5$$

Answer £   152.50

7 **(b)**   His sales in Week 4 were half of his sales in Week 1

Zayn says,

"This means that my profit in Week 4 was half of my profit in Week 1"

Is he correct?

You **must** show your working.

[2 marks]

Week 4 profit → £120 − £87.50 = £32.50

Incorrect because $\dfrac{£152.5}{2} = £76.25 \neq £32.50$

8   Work out the value of $5x + 9y$ when $x = 7$ and $y = -2$

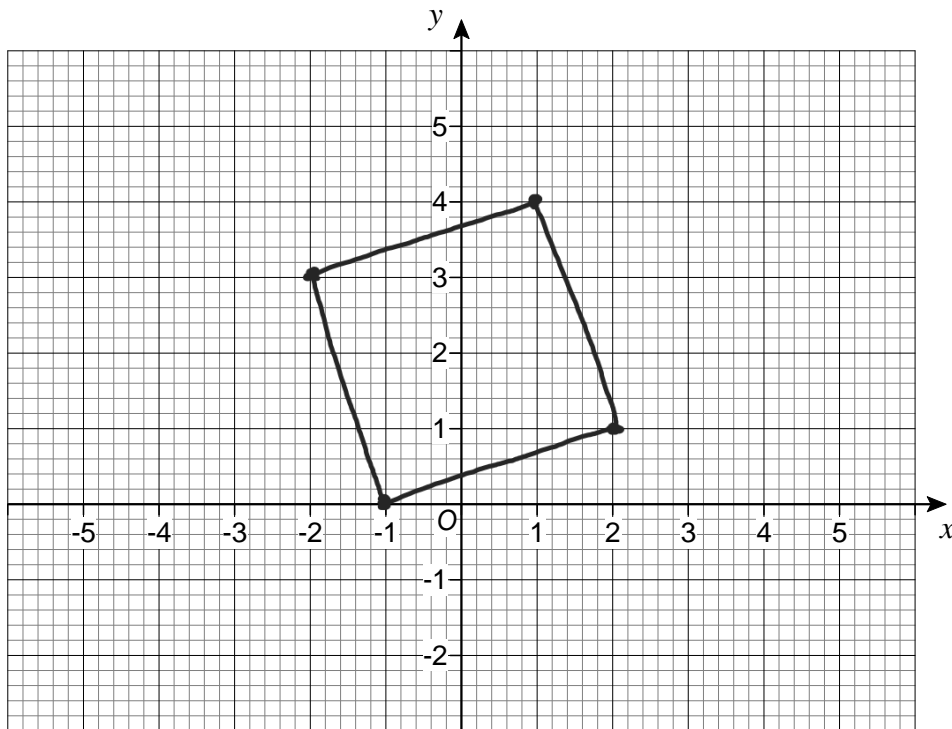**[2 marks]**

$$5(7) + 9(-2)$$
$$35 - 18 = \underline{17}$$

Answer   17

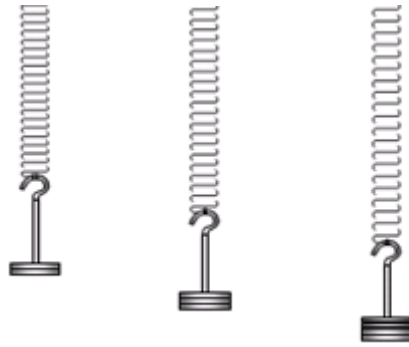**9**   The points $(-1, 0)$ and $(1, 4)$ are the diagonally opposite corners of a square.

Work out the coordinates of the other **two** corners of the square.

[2 marks]

Answer (**-2**   ,   **3**   ) and (**2**   ,   **1**   )

Turn over ▶

10 In an experiment, different masses are hung on a spring.

The length of the spring is measured for each mass.

Mass (g)	10	20	30	40
Length (cm)	20.8	21.6	22.4	23.2

10 (a) Draw a graph to show the length of the spring for masses from 10 g to 40 g

[2 marks]
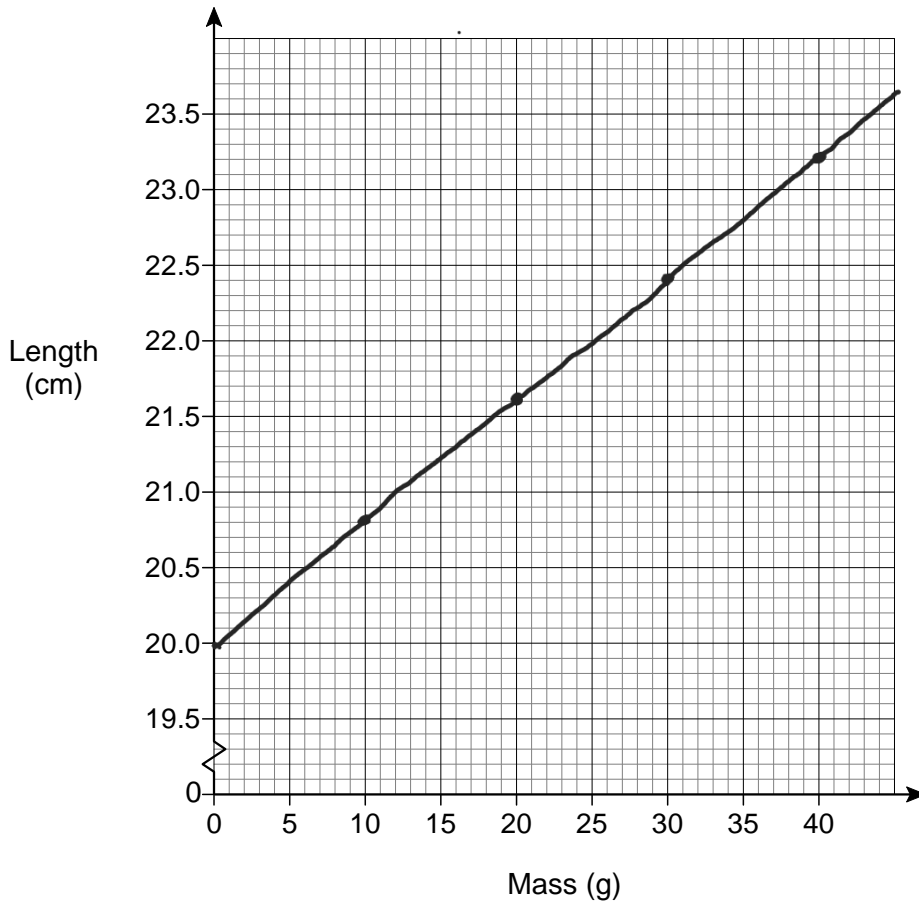
10 (b) Estimate the length of the spring with no mass hung on it.

[1 mark]

Answer _____ 20 _____ cm

10 (c) How much longer is the spring with a 35 g mass than with a 15 g mass?

[2 marks]

35g → 22.8cm
15g → 21.2cm
22.8 − 21.2 = 1.6 cm

Answer _____ 1.6 _____ cm

Turn over for the next question

11 A sequence of patterns uses grey squares and white squares.

Here are the first four patterns.

Pattern 1   Pattern 2   Pattern 3   Pattern 4

6   9   12   15
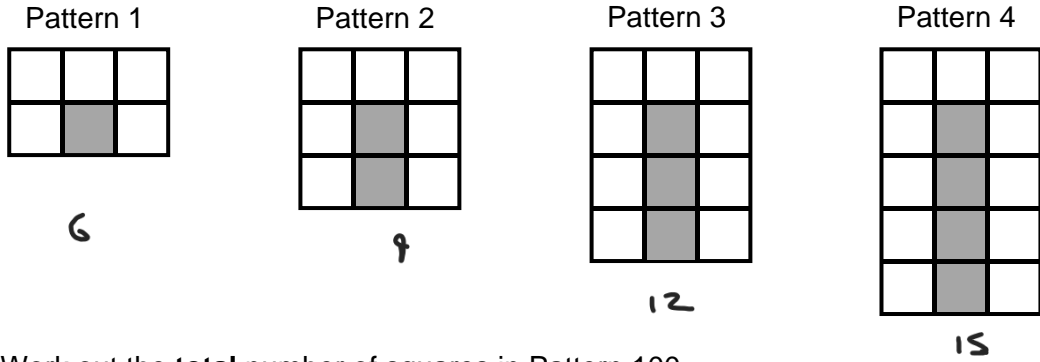
11 (a) Work out the **total** number of squares in Pattern 100

[3 marks]

Should be 101th number in 3 times table

101 × 3 = 303

Answer ___303___

11 (b) Complete this number machine for the sequence of patterns.

[1 mark]

Number of
grey squares → | × **2** | →→ | + **3** | → Number of
white squares
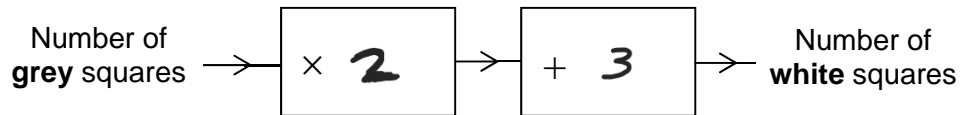
Turn over for the next question

12 In Scotland, squirrels are red or grey in the ratio red : grey $= 1 : 2\frac{1}{2}$

12 (a) What fraction of the squirrels in Scotland are red?

[2 marks]

$$red = \frac{1}{1+2\frac{1}{2}} = \frac{1}{3\frac{1}{2}} = \frac{2}{7}$$

Answer _____2/7_____

12 (b) In Scotland there are 120 000 red squirrels.

How many squirrels are there altogether in Scotland?

[2 marks]

$$120\,000 = \frac{2}{7}$$

$$\frac{120\,000}{2} \times 7 = total = 420,000$$

Answer _____420,000_____

13 Hayley and Tom have £2000 to spend on food at their wedding.

Here are their two options.

Wonderful Weddings!

Normal price   £32 per person

Special offer

10% off

Kim the Caterer

Number of people	Price per person
100 & over	£24.50
80 to 99	£26.50
60 to 79	£28.50
up to 59	£30.50

Work out the **maximum** number of people they can pay for.

Show working to compare the maximum number of people for **both** options.

[5 marks]

Wonderful weddings → £32 × 0.9 = £28·80 per person

$\frac{£2000}{£28.80}$ = 69.4̇ so they can pay for 69

Caterer → 80 × £26.50 = £2120, which is over £2000

So will be in £28·50 pay range → $\frac{£2000}{£28.50}$ = 70.2
= 70 people

Maximum number if use caterer = 70

Answer   70

Turn over ▶

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14   Solve $4(x + 5) = 15$

[3 marks]

$4x + 20 = 15$

$4x = -5$

$x = -5/4 = -1.25$

$x =$ -1.25

15   The mass of 40 cm^3 of copper is 356 grams.

Work out the mass of 90 cm^3 of copper.

[2 marks]

cm^3 : grams

$\div 4 \left(\begin{array}{l} 40 = 356 \\ 10 = 89 \end{array} \right) \div 4$

$\times 9 \left(90 = 801 \right) \times 9$

Answer _____ 801 _____ grams

16 24 boys, 45 girls and 281 adults are the members of a badminton club.

50 more children join the club.

The number of girls is **now** 18% of the total number of members.

How many of the 50 children were **boys**?

[4 marks]

24 + 45 + 281 + 50 new = 400 members

$\frac{18}{100} \times 400 = 72$ girls

72 − 45 = 27 new girls

50 − 27 = 23 new boys

Answer ___23___

Turn over for the next question

17 The table shows information about the marks of 30 students in a test.

Mark	Frequency
14	2
15	10
16	2
17	3
18	13
	Total $= 30$

Students who scored less than the mean mark have to retake the test.

How many students have to retake the test?

You **must** show your working.

[3 marks]

$$\text{Mean} = \frac{(2 \times 14) + (2 \times 16) + (10 \times 15) + (3 \times 17) + (13 \times 18)}{30}$$

$$= \frac{495}{30} = \underline{16 \cdot 5 \text{ marks}}$$

So people who got 14, 15, 16 have to retake $= 2 + 10 + 2 = \underline{\underline{14}}$

Answer _____ 14 _____

18 Work out the square root of 100 million.

Circle your answer.

[1 mark]

1000   10 000   100 000   1 000 000

$\sqrt{100,000,000}$

$= 10,000$

19 $\mathbf{a} = \begin{pmatrix} 5 \\ -2 \end{pmatrix}$ and $\mathbf{b} = \begin{pmatrix} -2 \\ 3 \end{pmatrix}$

Circle the vector $\mathbf{a} - \mathbf{b}$

[1 mark]

$\begin{pmatrix} -3 \\ -5 \end{pmatrix}$ $\begin{pmatrix} 7 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 3 \\ 1 \end{pmatrix}$ $\begin{pmatrix} 7 \\ -5 \end{pmatrix}$

$\begin{pmatrix} 5 \\ -2 \end{pmatrix} - \begin{pmatrix} -2 \\ 3 \end{pmatrix} = \begin{pmatrix} 7 \\ -5 \end{pmatrix}$

20 Circle the decimal that is closest in value to $\dfrac{2}{3}$

[1 mark]

0.6   0.66   0.667   0.67

$2/3 = 0.\dot{6} = 0.6666 \ldots$

so 0.667 closest

Turn over for the next question

21 When $x^2 = 16$ the **only** value that x can be is 4

Is this true or false?

Tick a box.

[1 mark]

True ☐   False ☑

Reason <u>Could be −4 also</u>
$$-4 \times -4 = 16$$
$$\sqrt{16} = \pm 4$$

22 In 1999 the minimum wage for adults was £3.60 per hour.

In 2013 it was £6.31 per hour.

Work out the percentage increase in the minimum wage.
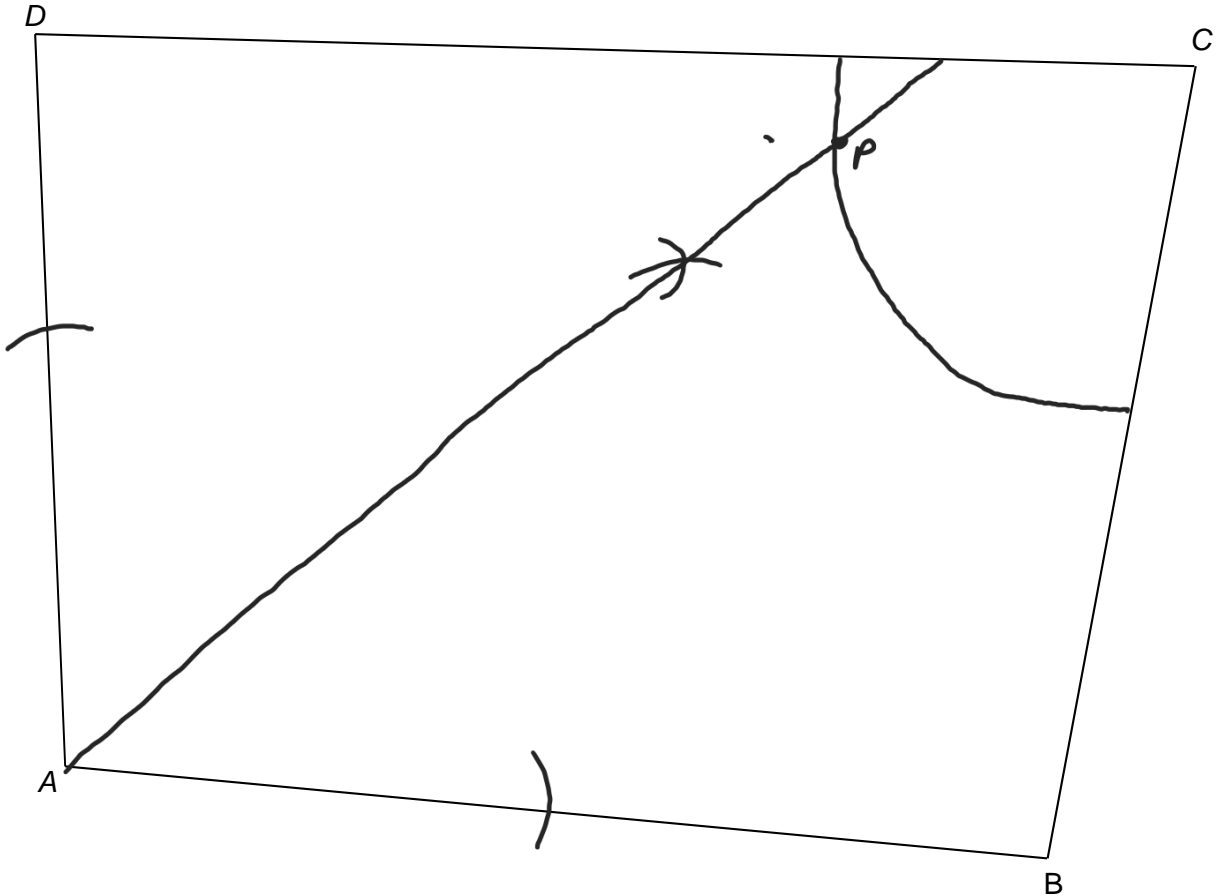
[3 marks]

$$\frac{£6 \cdot 31}{£3 \cdot 60} = 1.7527$$
$$= 75 \cdot 3 \%$$

Answer **75.3** %

23   Use ruler and compasses to answer this question.

Point *P* is

- the same distance from *AB* and *AD*
- 6 cm from *C*.

Show the position of *P* on the diagram.

[3 marks]

① First draw angle bisector of ∠DAB

② Then draw 6cm radius from C.

P is point they cross each other as they met both conditions.

Turn over for the next question

24 (a) Use your calculator to work out $19.42^2 - \sqrt[3]{1006} \div 4.95$

Write down your full calculator display.

[1 mark]

$$(19.42)^2 - \left(\sqrt[3]{1006} \div 4.95\right)$$

$$= 375.1121656$$

Answer $\underline{375.1121656}$

24 (b) Use approximations to check that your answer to part (a) is sensible.

You **must** show your working.

[2 marks]

$19.42 \simeq 20$

$1006 \simeq 1000$ } 1st

$4.95 \simeq 5$

$(20)^2 - \dfrac{\sqrt[3]{1000}}{5} = 398$

25   Three cups, A, B and C, contain only salt and water.

The different mixtures are

        A   salt : water $= 3 : 22$

        B   salt $= \dfrac{1}{8}$

        C   salt $= 12.75\%$

Which cup has the greatest proportion of salt?

You **must** show your working.

[3 marks]

$$A \rightarrow \overset{S\ \ W}{3:22} \rightarrow \frac{3}{25} = 0.1200$$

$$B \rightarrow \longrightarrow 1/8 = 0.1250$$

$$C \longrightarrow 12.75\% = 0.1275$$

So C has most

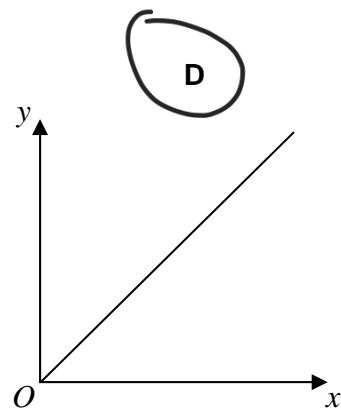Answer   C

Turn over for the next question

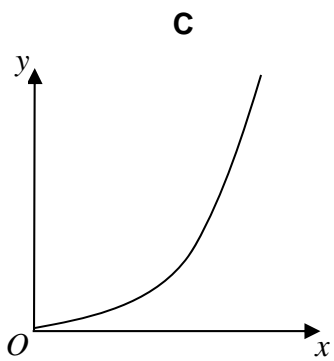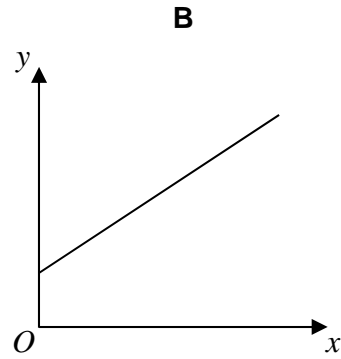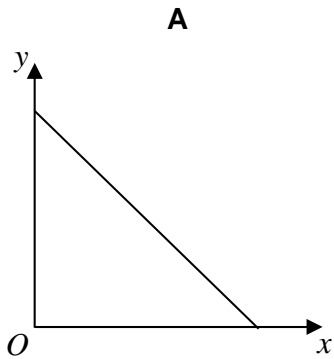**26** y is directly proportional to x.

Which graph shows this?
Circle the correct letter.

[1 mark]

A

B

C

D

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27   A bag contains counters that are red, blue, green or yellow.

	red	blue	green	yellow
Number of counters	9	$3x$	$x-5$	$2x$

A counter is chosen at random.

The probability it is **red** is $\dfrac{9}{100}$

Work out the probability it is green.

[4 marks]

$$\text{Red} \rightarrow \frac{9}{100} = \frac{9}{9+3x+x-5+2x} = \frac{9}{9+6x-5} = \frac{9}{6x+4}$$

$$\text{So} \quad 6x+4=100 \quad \rightarrow \quad 6x=96$$
$$x=16$$

$$\text{Green} \rightarrow x-5$$
$$16-5=11$$

$$\text{So} \quad \frac{11}{100}$$

Answer $\dfrac{11}{100}$

Turn over for the next question

28 The pressure at sea level is 101 325 Pascals.

Any rise of 1 km above sea level decreases the pressure by 14%

For example,

at 3 km above sea level the pressure is 14% less than at 2 km

Work out the pressure at 4 km above sea level.

Give your answer to 2 significant figures.

[4 marks]

$1 - 0.14 = 0.86$ So   86% pressure left each km you go up

$101325 \times (0.86)^4 = 55425.6$ pascals

$= 55,000$ pascals

Answer _____55,000_____ Pascals

29 *ABC* is a triangle with *AB* = *AC*

BA is parallel to *CD*.

Not drawn accurately

A

D

P

x

15°

B

C
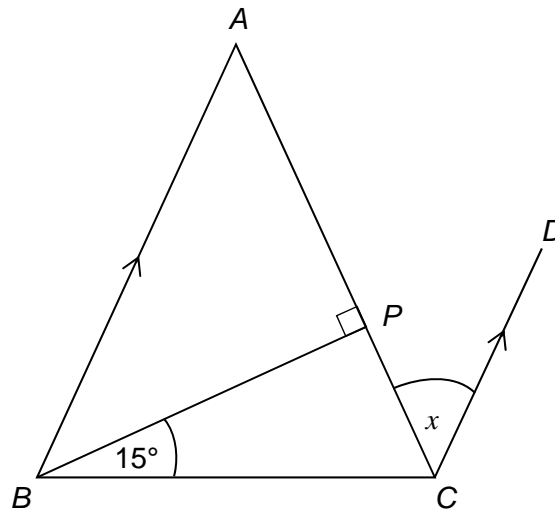
Show that angle *x* = 30°

[3 marks]

∠PCB = 75° because 180 − (90 + 15) = 75° and triangle angles add to 180°.

∠ABP = 75 − 15 = 60° because AC = AB, so triangle ABC is an isoceles making base angles equal.

$$180 = 75 + (75 + x)$$
$$180 - 150 = x$$
$$= 30$$

END OF QUESTIONS

There are no questions printed on this page

DO NOT WRITE ON THIS PAGE
ANSWER IN THE SPACES PROVIDED

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