

## Cambridge IGCSE<sup>™</sup>

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
ADDITIONAL MATHEMATICS 0606/22		
Paper 2		October/November 2020
		2 hours

You must answer on the question paper.

No additional materials are needed.

#### **INSTRUCTIONS**

- Answer all questions. •
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs. •
- Write your name, centre number and candidate number in the boxes at the top of the page. •
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid. •
- Do not write on any bar codes.
- You should use a calculator where appropriate. •
- You must show all necessary working clearly; no marks will be given for unsupported answers from a • calculator.

This document has 16 pages. Blank pages are indicated.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in • degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

[Turn over



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2 hours

### Mathematical Formulae

## 1. ALGEBRA

Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Binomial Theorem** 

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ 

Arithmetic series 
$$u_n = a + (n-1)d$$
  
$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a + (n-1)d\}$$

Geometric series

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \quad (|r| < 1)$$

#### 2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for  $\triangle ABC$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

## 1 Solve the inequality (x-8)(x-10) > 35.

[4]

# 2 Find the value of x such that $\frac{4^{x+1}}{2^{x-1}} = 32^{\frac{x}{3}} \times 8^{\frac{1}{3}}$ .

[4]

3 (a) Find the equation of the perpendicular bisector of the line joining the points (12, 1) and (4, 3), giving your answer in the form y = mx + c. [5]

(b) The perpendicular bisector cuts the axes at points *A* and *B*. Find the length of *AB*. [3]

4 Solve the simultaneous equations.

$$log_{3}(x+y) = 2$$
  

$$2log_{3}(x+1) = log_{3}(y+2)$$
[6]

## 5 DO NOT USE A CALCULATOR IN THIS QUESTION.

(a) Find the equation of the tangent to the curve  $y = x^3 - 6x^2 + 3x + 10$  at the point where x = 1. [4]

(b) Find the coordinates of the point where this tangent meets the curve again. [5]

[6]

7

6 Find the exact value of  $\int_2^4 \frac{(x+1)^2}{x^2} dx$ .

- 7 A geometric progression has a first term of 3 and a second term of 2.4. For this progression, find
  - (a) the sum of the first 8 terms,

[3]

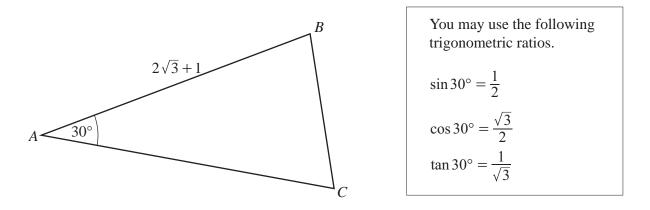
(**b**) the sum to infinity,

[1]

(c) the least number of terms for which the sum is greater than 95% of the sum to infinity. [4]

## 8 DO NOT USE A CALCULATOR IN THIS QUESTION.

In this question lengths are in centimetres.

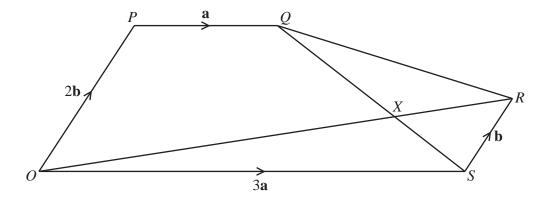


(a) Given that the area of the triangle *ABC* is  $5.5 \text{ cm}^2$ , find the exact length of *AC*. Write your answer in the form  $a + b\sqrt{3}$ , where a and b are integers. [4]

(b) Show that  $BC^2 = c + d\sqrt{3}$ , where c and d are integers to be found. [4]

[1]

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In the diagram  $\overrightarrow{OP} = 2\mathbf{b}$ ,  $\overrightarrow{OS} = 3\mathbf{a}$ ,  $\overrightarrow{SR} = \mathbf{b}$  and  $\overrightarrow{PQ} = \mathbf{a}$ . The lines *OR* and *QS* intersect at *X*. (a) Find  $\overrightarrow{OQ}$  in terms of **a** and **b**. [1]

(**b**) Find  $\overrightarrow{QS}$  in terms of **a** and **b**.

(c) Given that  $\overrightarrow{QX} = \mu \overrightarrow{QS}$ , find  $\overrightarrow{OX}$  in terms of **a**, **b** and  $\mu$ . [1]

(d) Given that 
$$\overrightarrow{OX} = \lambda \overrightarrow{OR}$$
, find  $\overrightarrow{OX}$  in terms of **a**, **b** and  $\lambda$ . [1]

(e) Find the value of  $\lambda$  and of  $\mu$ .

[3]

(f) Find the value of  $\frac{QX}{XS}$ .

(g) Find the value of  $\frac{OR}{OX}$ .

[1]

- 10 The number, *b*, of bacteria in a sample is given by  $b = P + Qe^{2t}$ , where *P* and *Q* are constants and *t* is time in weeks. Initially there are 500 bacteria which increase to 600 after 1 week.
  - (a) Find the value of P and of Q.

[4]

[1]

(b) Find the number of bacteria present after 2 weeks.

(c) Find the first week in which the number of bacteria is greater than 1 000 000. [3]

14

11 (a) Show that  $\frac{\sin x \tan x}{1 - \cos x} = 1 + \sec x.$ 

[4]

(b) Solve the equation  $5 \tan x - 3 \cot x = 2 \sec x$  for  $0^\circ \le x \le 360^\circ$ . [6]

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