

Cambridge IGCSE[™]

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

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ADDITIONAL MATHEMATICS

0606/21

Paper 2 October/November 2020

2 hours

You must answer on the question paper.

No additional materials are needed.

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Blank pages are indicated.

Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

Arithmetic series
$$u_n = a + (n-1)d$$

$$S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\left\{2a + (n-1)d\right\}$$

Geometric series
$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \ (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \ (|r| < 1)$$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

1 Solve the inequality |3x+2| > 8+x.

[3]

2 Find the coordinates of the points of intersection of the curve $x^2 + xy = 9$ and the line $y = \frac{2}{3}x - 2$.

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3 Write $3 \lg x + 2 - \lg y$ as a single logarithm. [3]

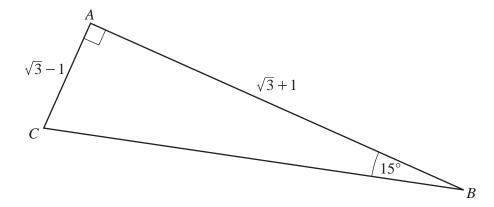
4 It is given that $y = \ln(\sin x + 3\cos x)$ for $0 < x < \frac{\pi}{2}$. (a) Find $\frac{dy}{dx}$.

(b) Find the value of x for which $\frac{dy}{dx} = -\frac{1}{2}$. [3]

5 The first three terms in the expansion of $(a+bx)^5(1+x)$ are $32-208x+cx^2$. Find the value of each of the integers a, b and c.

6 DO NOT USE A CALCULATOR IN THIS QUESTION.

In this question all lengths are in centimetres.



In the diagram above $AC = \sqrt{3} - 1$, $AB = \sqrt{3} + 1$, angle $ABC = 15^{\circ}$ and angle $CAB = 90^{\circ}$.

(a) Show that
$$\tan 15^{\circ} = 2 - \sqrt{3}$$
. [3]

7 DO NOT USE A CALCULATOR IN THIS QUESTION.

$$p(x) = 2x^3 - 3x^2 - 23x + 12$$

(a) Find the value of $p(\frac{1}{2})$. [1]

(b) Write p(x) as the product of three linear factors and hence solve p(x) = 0. [5]

8	The population P , in millions, of a country is given by $P = A \times b^t$, where t is the number of after January 2000 and A and b are constants. In January 2010 the population was 40 million an increased to 45 million by January 2013.							
	(a)	Show that $b = 1.04$ to 2 decimal places and find A to the nearest integer.	[4]					
	(b)	Find the population in January 2020, giving your answer to the nearest million.	[1]					
	(c)	In January of which year will the population be over 100 million for the first time?	[3]					
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9	A p	A particle moves in a straight line such that, t seconds after passing a fixed point O , its displacement from O is s m, where $s = e^{2t} - 10e^t - 12t + 9$.							
	(a)	Find expressions for the velocity and acceleration at time <i>t</i> .	[3]						
	(b)	Find the time when the particle is instantaneously at rest.	[3]						
	(c)	Find the acceleration at this time.	[2]						

- 10 The gradient of the normal to a curve at the point (x, y) is given by $\frac{x}{x+1}$.
 - (a) Given that the curve passes through the point (1, 4), show that its equation is $y = 5 \ln x x$. [5]

(b) Find, in the form y = mx + c, the equation of the tangent to the curve at the point where x = 3. [3]

11 The equation of a curve is $y = x\sqrt{16-x^2}$ for $0 \le x \le 4$.

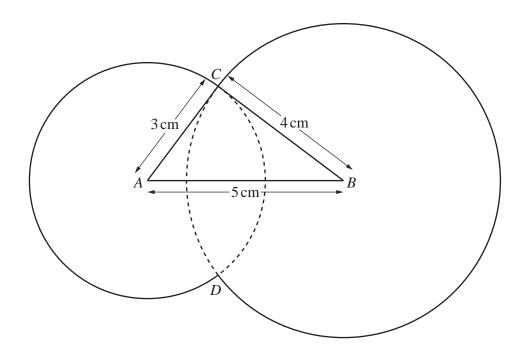
(a) Find the exact coordinates of the stationary point of the curve.

[6]

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(b) Find $\frac{d}{dx}(16-x^2)^{\frac{3}{2}}$ and hence evaluate the area enclosed by the curve $y = x\sqrt{16-x^2}$ and the lines y = 0, x = 1 and x = 3.

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The diagram shows a shape consisting of two circles of radius $3 \, \text{cm}$ and $4 \, \text{cm}$ with centres A and B which are $5 \, \text{cm}$ apart. The circles intersect at C and D as shown. The lines AC and BC are tangents to the circles, centres B and A respectively. Find

(a) the angle *CAB* in radians,

[2]

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(b) the perimeter of the whole shape, [4]

(c) the area of the whole shape. [4]

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