



**Cambridge International Examinations**  
Cambridge International General Certificate of Secondary Education

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**MATHEMATICS**

**0580/42**

Paper 42 (Extended)

**March 2017**

MARK SCHEME

Maximum Mark: 130

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**Published**

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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**Abbreviations**

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

Question	Answer	Marks	Part Marks
<b>1</b> (a)	22.9 or 22.85 to 22.86	2	<b>M1</b> for $\frac{8}{10+17+8} [\times 100]$ oe
	(b) $5635 \times \frac{17}{10+17+8}$ or better [= 2737]	2	<b>M1</b> for $\frac{5635}{(10+17+8)}$
	(c) 5000	3	<b>M2</b> for $5635 = k \left(1 + \frac{2.42}{100}\right)^5$ oe or <b>B1</b> for $\left(1 + \frac{2.42}{100}\right)$
	(d) 9950	2	<b>M1</b> for $2 \times 2500$ or $3 \times 1650$
	(e) 1.98 final answer	2	<b>B1</b> for 1.976 or 1.98 not final answer or <b>M1</b> for $130 \times 0.0152$
<b>2</b> (a) (i)	Rotation	1	
	90° [anticlockwise] oe	1	
	(9, 5)	1	
	(ii) Translation	1	
	$\begin{pmatrix} -8 \\ -14 \end{pmatrix}$ oe	1	
	(iii) Enlargement	1	
	[sf] $\frac{1}{3}$	1	
	(- 8, - 2)	1	
(b) (i)	Image at (1, - 3) (2, - 3) (2, - 5)	2	<b>M1</b> for triangle correct size and orientation, wrong position or <b>SC1</b> for correct reflection in $y = -x$
(ii)	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$	2	<b>B1</b> for 1 correct column or row

Question	Answer	Marks	Part Marks
<b>3</b> (a)	0 0.5 oe 1.25 oe	<b>1, 1, 1</b>	
(b)	Fully correct smooth curve	<b>4</b>	<b>B3 FT</b> for 7 or 8 points or <b>B2 FT</b> for 5 or 6 points or <b>B1 FT</b> for 3 or 4 points
(c)	3.6 to 3.8	<b>2</b>	<b>M1</b> for $y = 3.5$ soi
(d)	line $y = x + 1$ ruled  –1.55 to –1.40 4.55 to 4.8	<b>M1</b>  <b>A1 A1</b>	If 0 scored <b>SC1</b> for $y = x + 1$ stated or implied or for 2 correct values given
(e) (i)	Point plotted at (5, 5)	<b>1</b>	
(ii)	Tangent ruled from A	<b>1</b>	
(iii)	1.2 to 1.4	<b>B2</b>	<b>B2</b> and <b>M1</b> dep on reasonable attempt at tangent from (5, 5)  <b>M1</b> for change in $y$ / change in $x$ of <i>their</i> ruled line
<b>4</b> (a)	$\frac{1}{8}$ oe	<b>3</b>	<b>M2</b> for $\frac{1}{2}\left(1 - \frac{1}{6} - \frac{1}{4} - \frac{1}{3}\right)$ oe or <b>M1</b> for $\frac{1}{6} + \frac{1}{4} + \frac{1}{3}$ seen oe or idea that all sum to 1
(b)	$\frac{7}{12}$ oe	<b>2</b>	<b>M1</b> for $\frac{1}{3} + \frac{1}{4}$ oe
(c) (i)	$\frac{1}{16}$ oe	<b>2</b>	<b>M1</b> for $\frac{1}{4} \times \frac{1}{4}$ oe
(ii)	$\frac{2}{24}$ oe	<b>3</b>	<b>M2</b> for $2 \times \frac{1}{6} \times \frac{1}{4}$ oe or <b>M1</b> for $\frac{1}{6} \times \frac{1}{4}$ oe
(d)	12	<b>1</b>	

Question	Answer	Marks	Part Marks
<p><b>5 (a) (i)</b></p> <p><b>(ii)</b></p> <p><b>(b) (i)</b></p> <p><b>(ii)</b></p>	<p><math>(3x-1)(x+4)</math></p> <p><math>\frac{1}{3}</math> oe and <math>-4</math></p> <p><math>2 \times 2(x-4) - 2(2x+11) = (2x+11)(x-4)</math> or better</p> <p><math>2x^2 + 11x - 8x - 44</math> or better</p> <p><math>4x - 16 - 4x - 22 = 2x^2 - 8x + 11x - 44</math> <math>2x^2 + 3x - 6 = 0</math></p> <p><math>\frac{-3 \pm \sqrt{(3)^2 - 4(2)(-6)}}{2 \times 2}</math></p> <p><math>-2.64</math> and <math>1.14</math> final ans cao</p>	<p><b>2</b></p> <p><b>1</b></p> <p><b>M2</b></p> <p><b>B1</b></p> <p><b>A1</b></p> <p><b>2</b></p> <p><b>B1B1</b></p>	<p><b>M1</b> for <math>(3x+b)(x+c)</math> with <math>bc = -4</math> or <math>3c + b = 11</math> or for <math>3x(x+4) - 1(x+4)</math> or for <math>x(3x-1) + 4(3x-1)</math></p> <p><b>M1</b> for common denom <math>2(2x+11)(x-4)</math> seen or attempt to multiply through by denoms or for <math>\frac{2(x-4) - (2x+11)}{(2x+11)(x-4)} = \frac{1}{2}</math></p> <p>or for other correct relevant 2 bracket expansion if alt method used</p> <p>correct solution reached with all brackets expanded and no errors or omissions seen</p> <p><b>B1</b> for <math>\sqrt{(3)^2 - 4(2)(-6)}</math> or better or <math>\left(x + \frac{3}{4}\right)^2</math> oe and <b>B1</b> for <math>\frac{-3 + \sqrt{q}}{2(2)}</math> or <math>\frac{-3 - \sqrt{q}}{2(2)}</math> or better or <math>-\frac{3}{4} + \sqrt{\frac{57}{16}}</math> oe or <math>-\frac{3}{4} - \sqrt{\frac{57}{16}}</math> oe</p> <p><b>SC1</b> for <math>-2.6</math> or <math>-2.637\dots</math> <b>and</b> <math>1.1</math> or <math>1.137\dots</math> or <math>-2.64</math> and <math>1.14</math> seen in working or <math>2.64</math> and <math>-1.14</math> as final answers</p>
<p><b>6 (a) (i)</b></p> <p><b>(ii)</b></p> <p><b>(b)</b></p>	<p><math>27</math></p> <p><math>3.89</math> or <math>3.888</math> to <math>3.889</math></p> <p><math>76</math> cao</p>	<p><b>1</b></p> <p><b>2</b></p> <p><b>3</b></p>	<p><b>M1</b> for <math>\frac{7}{EZ} = \frac{9}{5}</math> oe</p> <p><b>B2</b> for <math>ABC = 104</math> or <math>AOC = 152</math> or <math>COD = 28</math> or <math>OBA = 52</math> <b>and</b> <math>OBC = 52</math> or <math>BCD = 128</math> <b>and</b> <math>OCB = 52</math> or <b>B1</b> for any one of <math>OBA, OBC, OCB = 52</math> or <math>BCD = 128</math></p>

Question	Answer	Marks	Part Marks
(c) (i)	90	1	
	angle in semicircle	1	
(ii)	27	1	
	tangent [perpendicular to] radius	1	
(iii)	rectangle	1	
7 (a)	72.7 or 72.70 to 72.71 nfw	4	<b>M1</b> for midpoints <b>soi</b> (condone 1 error or omission) (47.5, 55, 65, 80, 95, 110)  <b>M1</b> for use of $\sum fx$ with $x$ in correct interval including both boundaries (condone 1 further error or omission) (1092.5, 3520, 7930, 10880, 2470, 3190)  <b>M1</b> (dep on 2nd M1) for $\sum fx \div 400$
(b) (i)	[23] 87 209 345 371 [400]	2	<b>B1</b> for 2 or 3 correct
(ii)	Correct graph	3	<b>B1FT</b> <i>their</i> (b)(i) for 6 correct heights <b>B1</b> for 6 points at upper ends of intervals on correct vertical line <b>B1FT</b> (dep on at least B1) for increasing curve or polygon through 6 points  After 0 scored, <b>SC1FT</b> <i>their</i> (b)(i) for 5 correct points plotted
(iii) (a)	69 to 70	1	
(b)	20 to 23	2FT	<b>FT</b> <i>their</i> cumulative freq curve <b>M1</b> for correct UQ or LQ for <i>their</i> cumulative freq curve
(c)	72 to 75	2	<b>M1</b> for 240 <b>soi</b>
8 (a) (i)	5.14 or 5.135 to 5.142 nfw	4	<b>M2</b> for $[XY^2 =] 12.5^2 + 9.9^2 - 2 \times 12.5 \times 9.9 \times \cos 23$ or <b>M1</b> for implicit version <b>A1</b> for 26.4 to 26.5 OR <b>B1</b> for $[XYT = ] 108$ or $[TXY = ] 49$ <b>M2</b> for $\frac{12.5 \sin 23}{\sin(180 - 72)}$ oe or <b>M1</b> for $\frac{\sin(180 - 72)}{12.5} = \frac{\sin 23}{XY}$ oe

Question	Answer	Marks	Part Marks
(ii)	15.6 or 15.7 or 15.64 to 15.68	3	<b>M2</b> for $[TZ=]\frac{9.9}{\sin 37} \times \sin(72)$ oe or <b>M1</b> for $\frac{9.9}{\sin 37} = \frac{TZ}{\sin 72}$ oe OR <b>M2</b> for $\frac{12.5 \times \sin(180 - 23 - 108)}{\sin 37}$ oe or <b>M1</b> for $\frac{\sin 37}{12.5} = \frac{\sin(180 - 23 - 108)}{TZ}$ oe
(b)	3.79 or 3.793 to 3.794	4	<b>M3</b> for $r = 20.5 \div \left(2 + \frac{3 \times 65 \times 2\pi}{360}\right)$ oe or <b>M2</b> for $20.5 = 2r + \frac{3 \times 65}{360} \times 2\pi r$ oe or <b>M1</b> for $[3 \times] \frac{65}{360} \times 2\pi r$ oe or $20.5 = 2r +$ expression involving $\pi$
9 (a)	$x < 10$ oe $y \geq 2$ oe	1 1	Accept $x \leq 9$ Accept $y > 1$
(b)	$x + 3y \leq 21$ oe	1	Mark answer line isw
(c)	ruled broken line $x = 10$ ruled line $y = 2$ ruled line from (0, 7) to (21, 0) correct region indicated cao	<b>B1</b> <b>B1</b> <b>B2</b> 1	or ruled line $x = 9$ or ruled broken line $y = 1$ <b>SC1</b> for line with negative gradient correct only at (0, 7) or (21, 0)
(d) (i)	4	1	
(ii)	20	1	
10 (a) (i)	$(6 - 2) \times 180$ or $(2 \times 6 - 4) \times 90$ or $(360 \div 6)$ $(6 - 2) \times 180 \div 6$ or $(2 \times 6 - 4) \times 90 \div 6$ or $180 - (360 \div 6)$	<b>M1</b> <b>M1dep</b>	dep on previous M1
(ii)	$1.73x$ or $x\sqrt{3}$ oe	3	<b>M2</b> for $2x \sin 60$ or $2x \cos 30$ oe or for $\sqrt{x^2 + x^2} - 2 \times x \times x \times \cos 120$ or <b>M1</b> for $x \sin 60$ or $x \cos 30$ oe or for $x^2 + x^2 - 2 \times x \times x \times \cos 120$

Question	Answer	Marks	Part Marks
(iii)	$(10 - x)\sin 30$ seen oe	<b>M1</b>	
	$10 + 2((10 - x)\sin 30)$ oe	<b>M1dep</b>	dep on previous <b>M1</b>
	$10 + 10 - x$ or $10 + 2 \times \frac{1}{2} \times (10 - x)$	<b>A1</b>	with no errors or omissions seen
(b)	12.7 or 12.67 to 12.68.... nfw	<b>4</b>	<b>B3</b> for 7.32 to 7.33 or <b>M2</b> for $x = 20 \div (1 + 1.73)$ oe or <b>M1</b> for $20 - x = \textit{their (a)(ii)}$ oe
<b>11 (a)</b>	4 5 6 7 8 16 32 64 128	<b>1</b> <b>3</b>	<b>B2</b> for 3 or 4 correct or <b>B1</b> for first 2 correct If 0 scored, <b>SC1</b> for 4 values correctly doubled <b>FT</b> one error
(b)	$2^n$ oe	<b>1</b>	
(c) (i)	$2 + 4 + 8 = 14$ $16 - 2 = 14$	<b>1</b> <b>1</b>	or for $14 + 2 = 16 = 2^4$
(ii)	62 and 6	<b>2</b>	<b>B1</b> for each
(iii)	$2^{n+1} - 2$ oe	<b>1</b>	
(iv)	9	<b>1</b>	