

Cambridge International Examinations

Cambridge International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

* 9 2 4 2 8 1 9 0 7 7

ADDITIONAL MATHEMATICS

0606/12

Paper 1 February/March 2016

2 hours

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer **all** the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.



Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Binomial Theorem

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$

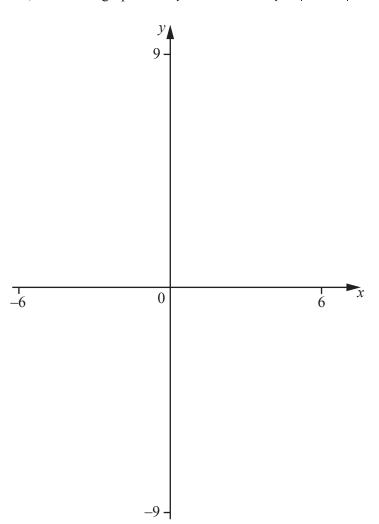
Find the values of a for which the line y = ax + 9 intersects the curve $y = -2x^2 + 3x + 1$ at 2 distinct points. [4]

2 Given that
$$\frac{p^{-2}qr^{-\frac{1}{2}}}{\sqrt{p^{\frac{1}{3}}q^2r^{-3}}} = p^aq^br^c$$
, find the values of a , b and c . [3]

3 Solve $\log_5 \sqrt{x} + \log_{25} x = 3$. [3]

4 (i) On the axes below, sketch the graphs of y = 2 - x and y = |3 + 2x|.





(ii) Solve |3+2x|=2-x.

[3]

(a)	A 6-character	passw	ord is	to be	chosen from the following 9 characters.	
	letters	A	В	Е	F	
	numbers	5	8	9		
	symbols	*	\$			
	Each characte	er may	be use	ed only	once in any password.	
	Find the num	ber of	differe	ent 6-c	haracter passwords that may be chosen if	
	(i) there are	no res	strictio	ns,		[1]
	(ii) the passy	word n	nust co	onsist c	of 2 letters, 2 numbers and 2 symbols, in that order,	[2]
((iii) the passy	word n	nust sta	art and	finish with a symbol.	[2]

(b)	An examination consists of a section A, containing 10 short questions, and a section B, containing
	5 long questions. Candidates are required to answer 6 questions from section A and 3 questions
	from section B. Find the number of different selections of questions that can be made if

(i) there are no further restrictions, [2]

(ii) candidates must answer the first 2 questions in section A and the first question in section B. [2]

- 6 A function f is such that $f(x) = 6 + e^{4x}$ for $x \in \mathbb{R}$.
 - (i) Write down the range of f.

[1]

(ii) Find $f^{-1}(x)$ and state its domain and range.

[4]

(iii) Find f'(x).

[1]

(iv) Hence find the exact solution of f(x) = f'(x).

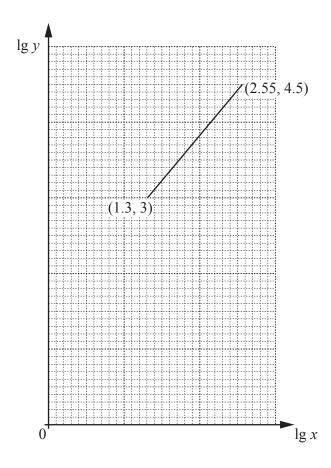
[2]

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- 7 The polynomial $f(x) = ax^3 + 7x^2 9x + b$ is divisible by 2x 1. The remainder when f(x) is divided by x 2 is 5 times the remainder when f(x) is divided by x + 1.
 - (i) Show that a = 6 and find the value of b. [4]

(ii) Using the values from part (i), show that $f(x) = (2x - 1)(cx^2 + dx + e)$, where c, d and e are integers to be found. [2]

(iii) Hence factorise f(x) completely. [2]



The variables x and y are such that when $\lg y$ is plotted against $\lg x$ the straight line graph shown above is obtained.

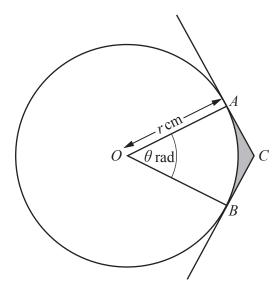
(i) Given that $y = Ax^b$, find the value of A and of b. [5]

(ii) Find the value of $\lg y$ when x = 100. [2]

(iii) Find the value of x when y = 8000. [2]

PMT

9



The diagram shows a circle, centre O, radius r cm. Points A, B and C are such that A and B lie on the circle and the tangents at A and B meet at C. Angle $AOB = \theta$ radians.

(i) Given that the area of the major sector AOB is 7 times the area of the minor sector AOB, find the value of θ . [2]

(ii) Given also that the perimeter of the minor sector *AOB* is 20 cm, show that the value of *r*, correct to 2 decimal places, is 7.18. [2]

(iii) Using the values of θ and r from parts (i) and (ii), find the perimeter of the shaded region ABC. [3]

(iv) Find the area of the shaded region *ABC*.

[3]

10 (i) Find
$$\frac{d}{dx} \left(x(2x-1)^{\frac{3}{2}} \right)$$
. [3]

(ii) Hence, show that
$$\int x(2x-1)^{\frac{1}{2}} dx = \frac{(2x-1)^{\frac{3}{2}}}{15}(px+q)+c$$
, where c is a constant of integration, and p and q are integers to be found. [6]

(iii) Hence find
$$\int_{0.5}^{1} x(2x-1)^{\frac{1}{2}} dx$$
. [2]

Question 11 is printed on the next page.

11 (i) Show that
$$\frac{1}{\csc \theta - 1} - \frac{1}{\csc \theta + 1} = 2 \tan^2 \theta$$
. [4]

(ii) Hence solve
$$\frac{1}{\csc \theta - 1} - \frac{1}{\csc \theta + 1} = 6 + \tan \theta \quad \text{for } 0^{\circ} < \theta < 360^{\circ}.$$
 [4]

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