


Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Pearson Edexcel		Centre Number			Candidate Number				
International GCSE		<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>			<input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/> <input type="text"/>				
Thursday 18 June 2020									
Morning (Time: 2 hours)					Paper Reference 4PM1/02				
Further Pure Mathematics									
Paper 2									
Calculators may be used.								Total Marks	

Instructions

- Use **black** ink or ball-point pen.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions.
- Without sufficient working, correct answers may be awarded no marks.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You must **NOT** write anything on the formulae page.
Anything you write on the formulae page will gain NO credit.

Information

- The total mark for this paper is 100.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Check your answers if you have time at the end.

Turn over ►

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Pearson

International GCSE in Further Pure Mathematics Formulae sheet

Mensuration

Surface area of sphere = $4\pi r^2$

Curved surface area of cone = $\pi r \times$ slant height

Volume of sphere = $\frac{4}{3}\pi r^3$

Series

Arithmetic series

Sum to n terms, $S_n = \frac{n}{2}[2a + (n-1)d]$

Geometric series

Sum to n terms, $S_n = \frac{a(1-r^n)}{(1-r)}$

Sum to infinity, $S_\infty = \frac{a}{1-r} \quad |r| < 1$

Binomial series

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \dots + \frac{n(n-1)\dots(n-r+1)}{r!}x^r + \dots \quad \text{for } |x| < 1, n \in \mathbb{Q}$$

Calculus

Quotient rule (differentiation)

$$\frac{d}{dx} \left(\frac{f(x)}{g(x)} \right) = \frac{f'(x)g(x) - f(x)g'(x)}{[g(x)]^2}$$

Trigonometry

Cosine rule

In triangle ABC : $a^2 = b^2 + c^2 - 2bc \cos A$

$$\tan \theta = \frac{\sin \theta}{\cos \theta}$$

$$\sin(A+B) = \sin A \cos B + \cos A \sin B$$

$$\sin(A-B) = \sin A \cos B - \cos A \sin B$$

$$\cos(A+B) = \cos A \cos B - \sin A \sin B$$

$$\cos(A-B) = \cos A \cos B + \sin A \sin B$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$\tan(A-B) = \frac{\tan A - \tan B}{1 + \tan A \tan B}$$

Logarithms

$$\log_a x = \frac{\log_b x}{\log_b a}$$

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- 2 The region enclosed by the curve with equation $y = e^{3x}$, the x -axis, the y -axis and the line with equation $x = 3$ is rotated through 360° about the x -axis.

Use algebraic integration to find, in terms of π and e , the volume of the solid generated.

(4)

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Question 2 continued

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(Total for Question 2 is 4 marks)



Question 3 continued

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(Total for Question 3 is 5 marks)



4 (i) Solve the equation $16\log_r 4 = \log_4 r$ (2)

(ii) Solve the equation $\log_5 9 + \log_5 12 + \log_5 15 + \log_5 18 = 1 + \log_5 x + \log_5 x^2$ (5)

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Question 4 continued

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(Total for Question 4 is 7 marks)



Question 5 continued

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(Total for Question 5 is 8 marks)



6

$$f(x) = 4x^2 - 3x - 5$$

The equation $f(x) = 0$ has roots α and β

Without solving the equation $f(x) = 0$

- (a) form an equation, with integer coefficients, that has roots $\frac{2\alpha}{\beta}$ and $\frac{2\beta}{\alpha}$ (6)

$$g(x) = 4x^2 + px + q \quad \text{where } p \text{ and } q \text{ are constants}$$

Given that the equation $g(x) = 0$ has roots $3\alpha + \beta$ and $\alpha + 3\beta$

- (b) find the value of p and the value of q (5)

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Question 6 continued

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Question 6 continued

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(Total for Question 6 is 11 marks)



Question 7 continued

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 12 marks)



Question 8 continued

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 15 marks)



Question 9 continued

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Question 9 continued

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Question 9 continued

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(Total for Question 9 is 18 marks)



10 (a) Show that

$$\cos(A + B) + \cos(A - B) = 2 \cos A \cos B \quad (2)$$

(b) Hence show that

$$\cos P + \cos Q = 2 \cos \frac{P + Q}{2} \cos \frac{P - Q}{2} \quad (3)$$

(c) Solve, for $0 \leq \theta \leq \frac{\pi}{2}$, the equation

$$\cos 5\theta + \cos 7\theta = 0$$

Give each solution in terms of π (4)

(d) Show that

$$\cos 8x + 2 \cos 6x + \cos 4x = 4 \cos 6x \cos^2 x \quad (3)$$

(e) Use calculus to find the exact value of

$$\int_0^{\frac{\pi}{3}} \cos 6x \cos^2 x \, dx \quad (4)$$

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Question 10 continued

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Question 10 continued

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