wjec cbac

GCSE MARKING SCHEME

SUMMER 2019

GCSE MATHEMATICS – UNIT 2 (HIGHER TIER) 3300U60-1

INTRODUCTION

This marking scheme was used by WJEC for the 2019 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

WJEC GCSE MATHEMATICS

SUMMER 2019 MARK SCHEME

GCSE MATHEMATICS	Mark	Comments
Unit 2 : Higher Tier1.(a)3n + 5 or equivalent	B2	B1 for sight of 3n. B0 for −3n Mark final answer.
1.(b) $3t = r + 8$ or $r + 8 = 3t$ or $-3t = -r - 8$ $t = \frac{r + 8}{3}$ or $\frac{r + 8}{3} = t$ or $t = \frac{-r - 8}{-3}$	B1 B1	F.T. only from $3t = \pm r \pm 8$, stated or implied. (3t = r + 8 will have already gained the previous B1.) B1B0 for $-t = -r - 8$ or equivalent. Mark final answer. <u>Note</u> Allow B1B0 for $t = (r + 8) \div 3$ with or without brackets. Allow B1B0 for $r + 8$ ('t' missing) 3
1.(c) $6x + 4 = 46$ OR $3x + 2 = 23$	B2	B1 for $(x + 5) + (2x - 3) + (x + 5) + (2x - 3) = 46$ or equivalent e.g. $(x + 5) + (2x - 3) = 23$
6x = 42 OR 3x = 21 (x =) 7	B1 B1	FT collection of 'their terms' if of equivalent difficulty. (linear equation only.) FT <u>only</u> from $ax = b$. Allow a fraction from a FT value unless x is a whole number. (x =) 7 gains all four marks. Each B mark implies all previous B marks. Mark final answer.
1.(c) <u>Alternative method</u> A trial showing correct values and understanding of perimeter. (e.g. $2(4 + 5) + 2(2 \times 4 - 3) = 28$) An i <u>mproved</u> trial. (x =)7	B1 B1 B2	Consistent use of x AND correct evaluation. Dependent on first B1. If 1 st trial is using '7' award B1B1 followed by B1 if left embedded but B2 if shown as $x = 7$. B1 for an implied / embedded ' $x = 7$ ' but not shown
		as x = 7. (x =) 7 gains all four marks. Mark final answer.

PMT

2. Intent to square at least two of the three	S1	(Note:
values.		$12 \cdot 8^2 = 163 \cdot 84$, $22 \cdot 7^2 = 515 \cdot 29$ and $25 \cdot 6^2 = 655 \cdot 36$)
Comparing $(25 \cdot 6)^2$ with $(12 \cdot 8)^2 + (22 \cdot 7)^2$ or Any intent to compare any other relevant values. (e.g. $(25 \cdot 6)^2 - (22 \cdot 7)^2$ with $(12 \cdot 8)^2$ or $\sqrt{[(12 \cdot 8)^2 + (22 \cdot 7)^2]}$ (with 25 \cdot 6))	M1	The comparison attempted must show <u>both</u> intended calculations e.g. $(25 \cdot 6)^2$ AND $(12 \cdot 8)^2 + (22 \cdot 7)^2$ unless intention is to compare with a given side e.g. $\sqrt{[(12 \cdot 8)^2 + (22 \cdot 7)^2]}$ with 25.6
Correct evaluation of value(s) to be compared. (e.g 'sight of 655·36 WITH 679·13' or 'sight of 140·07 WITH 163·84' or 'sight of 26·06 (WITH 25·6)')	A1	C.A.O. but allow evaluated answers to be given to the nearest whole number. e.g. 655 WITH 679.
Statement that it is NOT possible	A1	Allow FT if M1 awarded. If all marks gained ISW.
2. <u>Alternative method 1</u> Intent to use two right-angled trig ratios using 2 <u>different pairs</u> of given sides	S1	<i>i.e. In order to find the value of either the same angle OR two different angles, whilst sufficient to show that it isn't a right-angled triangle.</i>
 Correct right-angled trig ratio used twice, using 2 <u>different given sides</u>, in order to compare the values of the same angle or the sum of the two angles with 90°. 	M1	
Correct evaluation of value(s) to be compared.	A1	CAO
e.g. sight of any two of 30(°), 27.5(°) and 29.4(°)		Ratio Opp Adj Hyp Angle
OR sight of 30(°) and 60.58(°) (and the sum to be		Sin 12.8 25.6 30(°)
compared with 90°)		Cos 22.7 25.6 27.5(°)
		Tan 12.8 22.7 29.4(°)
		Sin 22.7 25.6 62.46(°)
		$\begin{array}{c c c c c c c c c c c c c c c c c c c $
		$\begin{array}{c ccccccccccccccccccccccccccccccccccc$
Statement that it is NOT possible	A1	If comparing the sum of two angles (with 90°), the sum must be shown. Allow FT if M1 awarded. If all marks gained ISW.
2. Alternative method 2 (using the cosine rule)		NOTE The cosine rule is not on the intermediate tier
$(\cos A =) (12.8^{2} + 22.7^{2} - 25.6^{2}) / (2 \times 12.8 \times 22.7)$ (= 2377/58112 or 0.0409)	М2	specification, but as it is a common question, it may be seen by Higher tier candidates. M1 for $25.6^2 = 12.8^2 + 22.7^2 - 2 \times 12.8 \times 22.7 \times \cos A$
(A =) 87(.6557°)	A1	
Statement that it is NOT possible	A1	
		If all marks gained ISW.

Organisation and Communication	OC1	For OC1, candidates will be expected to:
organisation and communication	001	present their response in a structured way
		• explain to the reader what they are doing at
		each step of their responselay out their explanation and working in a
		• lay out their explanation and working in a way that is clear and logical
		write a conclusion that draws together their
		results and explains what their answer means
		Inearis
Accuracy of writing.	W1	For W1, candidates will be expected to:
		show all their working
		 make few, if any, errors in spelling, punctuation and grammar
		 use correct mathematical form in their
		working
		 use appropriate terminology, units, etc
3.(a) $A \cap B$	B1	
3.(b) B	B1	P0 if all four original sumbars used
4 Four numbers with a range of 10.	B1	B0 if all four original numbers used.
Four numbers with a total of 36.	B1	
Four numbers with a median of 8.	B1	
Possible answers for all three marks are 5,5,11,15 or 5,6,10,15 or 5,7,9,15 or 5,8,8,15		
5. (number of females in Porth =) 90×128	M1	Or equivalent
360		
OR (number of males in Porth =) $\frac{120}{360} \times 72$		
(number of formalise in Dorth) 22	A 4	Answers may be seen on the diagram.
(number of females in Porth =) 32 (number of males in Porth =) 24	A1 A1	An answer of 32 implies M1. An answer of 24 implies M1.
()		
(Probability from Porth =) <u>56</u> or equivalent ISW 200	A1	FT ('their 32' + 'their 24') /200 provided M1 gained. Penalise incorrect notation -1. e.g. '56 in 200'.
6. $\sin(\text{QPR}) = 9.6$	M1	
16.7		
(QPR =) sin ⁻¹ (9.6/16·7) or sin ⁻¹ (0·57)	m1	Implies M1.
= 35.1(°) or 35.09(°) or 35.089(°)	A1	Allow any answer that rounds to 35(°)
6. <u>Alternative method.</u> Correct use of 'two-step' method.	M2	A partial trigonometric method is M0.
$(x) = 35.1(^{\circ}) \text{ or } 35.09(^{\circ}) \text{ or } 35.089(^{\circ})$	A1	Allow any answer that rounds to 35(°)
7. $7x + 2y = (\pounds)41.5(0)$ AND	B1	Allow use of other letters to denote variables.
$4x + 3y = (\pounds)29.75$		B0 for using 4150 and 2975.
		FT 'their equations' if of equal difficulty.
Method to eliminate variable	M1	Allow 1 error in one term, not one with equal
(Attempt at equal coefficients and subtraction)		coefficients.
First variable found $x = (\pounds) 5$ or $y = (\pounds)3.25$.	A1	C.A.O. (for their equations if FT.)
Substitute to find the 2 nd variable.	m1	F.T. their '1 st variable'.
Second variable found.	A1	ET anowers should be given to the present nearly
		FT answers should be given to the nearest penny (rounded or truncated).
		If M0, award SC2 (with possible B1) for both answers
		of (£) 5 AND (£)3.25.

8.		Correct evaluation regarded as enough to identify if
0.		'too high' or 'too low'. If evaluations not seen accept
		'too high' or 'too low'.
		<u>x</u> $2x^3 + x - 10$ (or check $2x^3 + x = 10$)
One correct evaluation $1 \le x \le 2$	B1	
2 correct evaluations $1.55 \le x \le 1.75$,	B1	1 -7
one < 0, one > 0.		1.1 -6.238
2 correct evaluations $1.55 \le x \le 1.65$,	M1	1.2 -5.344
one < 0, one > 0.		1.3 -4.306
		1·4 –3·112 1·45 – 2·452
x = 1.6	A1	1.5 -1.75 1.55 -1.002
		1·6 -0·208 1·65 0·634
		1.7 1.526 1.75 2.468
		1.8 3.464 $(1.62 0.123)$
		1.9 5.618 (1.63 0.291) 2 8 (1.64 0.461)
9. 85% ≡ 6154	B1	2 8 (1.64 0.461) Accept any indication.
$\begin{array}{ccc} 9. & 85\% = 6154 \\ & 6154 \times 100 \text{ OR } 6154 \end{array}$	M1	Implies the B1.
85 0.85		
= 7240	A1	
10. $x = 54(^{\circ})$	B1	
<u>Opposite angles</u> (of a) <u>cyclic quad</u> . (add up to 180°).	E1	Dependent on an attempt at 180 – 126.
y = 108(°)	B1	FT 2 \times 'their 54' only if less than 360°
Angle at the centre (is twice the angle at the	E1	Dependent on an attempt at $2 \times$ 'their 54'.
circumference).		
11. Correct enlargement	B2	Otherwise B1 for 2 correct vertices within a triangle.
		OR for 3 correct vertices in the correct location not
		joined to form the triangle
		OR triangle of correct shape, size and orientation in
		incorrect position
		OR consistent correct use of an incorrect negative
	D 0	scale factor.
12(a). $(9p+1)(9p-1)$	B2 B2	B1 for $(9p 1)(9p 1)$
12(b). $(7t-2)(t+3)$		B1 for $(7t \dots 2)(t \dots 3)$
13. Sight of 297.5 AND 6.5 297.5 ÷ 6.5	B1	Accept 6 hours 30 minutes, but not 6.3 hours.
297.5 ÷ 6.5	M1	If other calculations shown, then the relevant calculation must be identified.
		Award M1 for their values provided 295≤d<300 AND
		$6 \le 1 \le 7$ (but not 6 hours 30 minutes).
= 45.77(km/h)	A1	CAO. Correct answer must be clearly identified.
14. sin BAD = $(2\times70)/(8\times19)$ or equivalent	M2	Allow any unambiguous indication of angle BAD.
		M1 for the correct use of the formula when sinBAD is
		not the subject, for example: $70 = 1/2 \times 8 \times 19 \times 10^{-10}$
		,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,
(BAD=) 67(.08°)	A1	Allow any answer that rounds to 67(°).
		· · · · · · · · · · · · · · · · · · ·
(Area of sector ABD=) 67(.08)/360×π×8 ²	M1	Accept 292.9()/360×π×8 ² OR 293/360×π×8 ² for
		the erec of the major costor APD
		the area of the major sector ABD.
		FT their derived or stated value of angle BAD.
	-	FT their derived or stated value of angle BAD.
Accept answers in the range 37.4(cm ²) to 37.5(cm ²)	A1	FT their derived or stated value of angle BAD. Accept an answer in the range 163.5(cm ²) to
Accept answers in the range 37.4(cm ²) to 37.5(cm ²) OR 37(cm ²)	A1	FT their derived or stated value of angle BAD.

45	DO	D4 for env 4 or 0 correct
15. Graph Equation	B2	B1 for any 1 or 2 correct.
y = (x+1)(x-4)		
$y = (x-4)^2$		
y = x(x+4)		
y = (x - 1)(x + 4)		
y = (x - 2)(x + 2)		
y = x(x-4)		
$ \begin{array}{c} & & \\ \hline & & \\ & & \\ \end{array} $		
y = (1 - x)(x + 4)		
$y = (x+4)^2$		
16.(a) General sine curve with appropriate orientation and position.	M1	Ignore curve shown for values x< -180° or x> 180°.
-1 and 1 indicated on the y-axis, curve passes through $(-180^\circ,0)$, $(0^\circ,0)$ and $(180^\circ,0)$ and $(200^\circ,1)$	A1	
approximately (-90°,-1) and (90°,1). 16(b)30(°) AND -150(°)	B2	Accept embedded answers.
		Penalise further incorrect answer(s) -1.
		Ignore further answer(s) outside of the range.
		Award P1 for eight of an answer $20(\circ)$ or $150(\circ)$
		Award B1 for sight of an answer -30(°) or -150(°) (but not for sight of -30 as part of working).
17.(a) $\frac{3}{100} \times \frac{1}{99}$	M1	(but not for orginal of all part of monang).
$=\frac{3}{9900}\left(=\frac{1}{3300}\right)$ ISW	A1	Allow 3(.03)×10 ⁻⁴ OR 0.0003(03) or equivalent.
7700 (3300/		A0 for 0.0003(03)%.
		An unsupported 0.000303() gains M1A1. An unsupported 3/10000 OR 0.0003 gains no marks.
17(b) $2 \times \frac{3}{100} \times \frac{1}{99} \left(= \frac{6}{9900} = \frac{1}{1650} \right)$	M2	M1 for sight of $\left(\frac{3}{100} \times \frac{1}{99}\right) + \left(\frac{3}{100} \times \frac{1}{99}\right)$ OR
$+\frac{3}{100}\times\frac{2}{99}\left(=\frac{6}{9900}=\frac{1}{1650}\right)$		$\left(\frac{3}{100} \times \frac{1}{99}\right) + \left(\frac{1}{100} \times \frac{3}{99}\right) OR \ 2 \times \frac{3}{100} \times \frac{1}{99} OR$
OR $\frac{4}{100} \times \frac{3}{99}$		$ \left(\frac{3}{100} \times \frac{1}{99}\right) + \left(\frac{3}{100} \times \frac{2}{99}\right) $
$=\frac{12}{9900}\left(=\frac{1}{825}\right)$ ISW	A1	Allow 1(.21)×10 ⁻³ OR 0.001(21) or equivalent.
9900 (8257		An unsupported answer of 0.00121(2) gains M2A1. A0 for 0.001(21)%.
		SC1 for working with replacement leading to an
		answer of 12/10000 (3/2500) OR 0.001(2) [may be
		unsupported].

М2	$ \begin{array}{l} \text{M1 for sight of:} \\ \left[\left(\frac{96}{100} \times \frac{95}{99} \right) + \left(2 \times \frac{3}{100} \times \frac{96}{99} \right) + \left(2 \times \frac{1}{100} \times \frac{96}{99} \right) \right] \text{ OR} \\ 1 - \left[\left(\frac{96}{100} \times \frac{95}{99} \right) + \left(\frac{3}{100} \times \frac{96}{99} \right) + \left(\frac{1}{100} \times \frac{96}{99} \right) \right] \end{array} $
A1	Allow 1(.21)×10 ⁻³ OR 0.001(21) or equivalent. An unsupported answer of 0.00121(2) gains M2A1. A0 for 0.001(21)%. SC1 for working with replacement leading to an answer of 12/10000 (3/2500) OR 0.001(2) [may be unsupported].
M2	M1 for $23^2 = 13^2 + 17^2 - 2 \times 13 \times 17 \times \cos CAB$
A 4	
AT	SC1 for the correct evaluation of either of the two other angles. ABC = $33(.9)$ and ACB = $46(.8)$.
B1	Or equivalent.
B1 B1	Or equivalent. FT expansions of equivalent level of difficulty
ы	provided B1 previously awarded.
	'= 0' required, but may be implied by an attempt to
	use the quadratic formula or if $a = 8, b = -15$,
	c = 2 used in the quadratic formula.
M1	This substitution into the formula must be seen for M1.
	FT 'their derived quadratic equation' equated to zero of equivalent difficulty (a , b and c must be non-zero). Allow one slip in substitution <u>for M1 only</u> , but must be correct formula.
A1	Can be implied from at least one correct value of x evaluated.
A1	CAO for their quadratic equation but not if complex roots.
	M0A0A0 if trial and improvement used or for unsupported answers.
	May be seen in parts.
B2	Award B1 for a linear scale factor:
	$\sqrt{(199/47)}$ (= 2.057) OR $\sqrt{(47/199)}$ (= 0.485)
	or equivalent OR Award B1 for $(100/47)^3$ (- 75 004 -) OB
	Award B1 for (199/47) ³ (= 75.904) OR (47/199) ³ (= 0.013).
M1	(477100) (= 0.010).
A1	CAO. Not from premature approximation.
	VI2 A1 B1 B1 A1 A1 A1 B2 VI1

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