

Mark Scheme (Results)

Summer 2019

Pearson Edexcel International GCSE In Mathematics B (4MB1) Paper 01

#### **Edexcel and BTEC Qualifications**

Edexcel and BTEC qualifications are awarded by Pearson, the UK's largest awarding body. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information visit our qualifications websites at <a href="https://www.edexcel.com">www.edexcel.com</a> or <a href="https://www.edexcel.com">www.btec.co.uk</a>. Alternatively, you can get in touch with us using the details on our contact us page at <a href="https://www.edexcel.com/contactus">www.edexcel.com/contactus</a>.

## Pearson: helping people progress, everywhere

Pearson aspires to be the world's leading learning company. Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for our commitment to high standards and raising achievement through innovation in education. Find out more about how we can help you and your students at: <a href="https://www.pearson.com/uk">www.pearson.com/uk</a>

## General Marking Guidance

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded.
   Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

## Types of mark

- M marks: method marks
- A marks: accuracy marks
- B marks: unconditional accuracy marks (independent of M marks)

### Abbreviations

- o cao correct answer only
- o ft follow through
- isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- o awrt answer which rounds to
- o eeoo each error or omission

#### No working

If no working is shown then correct answers normally score full marks If no working is shown then incorrect (even though nearly correct) answers score no marks.

## With working

If there is a wrong answer indicated on the answer line always check the working in the body of the script (and on any diagrams), and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

If a candidate misreads a number from the question. Eg. Uses 252 instead of 255; method marks may be awarded provided the question has not been simplified. Examiners should send any instance of a suspected misread to review. If there is a choice of methods shown,

then no marks should be awarded, unless the answer on the answer line makes clear the method that has been used.

If there is no answer on the answer line then check the working for an obvious answer.

### Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. Incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially makes the answer incorrect eg algebra.

Transcription errors occur when candidates present a correct answer in working, and write it incorrectly on the answer line; mark the correct answer.

# Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded to another.

Question	ion	Working		Answer	Mark	Notes
1 (	(a)			8700	1	B1 oe
(	(b)			0.037	1	B1 oe
						Total 2 marks
2		$ 30 = 2 \times 3 \times 5 \qquad 30 = 6 \times 5  48 = 2^4 \times 3 \qquad 48 = 6 \times 8 $	2     18     30     48       3     9     15     24       3     5     8       2     18     30     48       2     9     15     24       2     9     15     12       2     9     15     6       3     9     15     3       3     3     5     1       5     1     5     1       1     1     1     1			M1 Prime factors for two of 18, 30, 48 (or equivalent) or lists multiples of 18, 30 and 48 (at least 2 multiples, not inc number itself for all three of the numbers, ie (18),36,54, (30),60,90, (48),96,144,) or table method
				720	2	A1
						Total 2 marks
3 (	(a)			Second row first square	1	B1 Or row four third square
	(b)			Second row third square	1	B1
		-				Total 2 marks
4		$\frac{9}{4} \times \frac{6}{23}$ or $\frac{9}{4} \div \frac{23}{6}$				M1 Or equivalent method for dividing two fractions
		$\frac{54}{92} = \frac{27}{46}$ or $\frac{9}{2} \times \frac{3}{23} = \frac{27}{46}$ or $\frac{9}{2} \div \frac{23}{3} = \frac{27}{46}$	$= \frac{27}{46} \text{ or } \frac{27}{12} \div \frac{46}{12} = \frac{27}{47} \text{ oe}$	$\frac{27}{46}$	2	A1 Dependent on all working seen
						Total 2 marks

Question	Working	Answer	Mark	Notes
5				M1 One term differentiated correctly
		$8x^3 + \frac{6}{x^3}$	2	A1 oe (e.g. $8x^3 + 6x^{-3}$ )
				Total 2 marks
6	$\frac{5-(-10)}{-3-2}$			M1 Condone one sign error or award if gradient of 3
		-3	2	A1
		·		Total 2 marks
7	$8x^2 + 12x - 10x - 15$			M1 Four terms seen with at least three correct (with signs) or two terms correct in a three term expression
		$8x^2 + 2x - 15$	2	A1 Correct answer with no working scores both marks. Do not ignore subsequent working.
		·		Total 2 marks
8	(24-5(3))+(24-5(10))			M1 Or both terms correct but not added. Terms are 9 and - 26
		-17	2	A1
		<u>.</u>	•	Total 2 marks
9	$\frac{360}{9}$ or $9n = 360$ or $180(n-2) = 171n$ oe			M1
		40		A1
	_			Total 2 marks
10	$7.60 \times 0.85$			M1 Or for working out 15% of £7.60 (=£1.14 or 114p) and taking away from £7.60 or 760. Units not needed
		£6.46	2	A1 accept 646p
			·	Total 2 marks

Que	stion	Working	Answer	Mark	Notes
11	(a)		$6x^7$	1	B1
	(b)				M1 for two terms correct as part of a product. Do not ISW
			$64a^6b^9$	2	A1
					Total 3 marks
12	(a)		C( ) > 2		B1 or $y \ge -2$ or $f \ge -2$ or set notation $[-1, \infty)$ or
			$f(x) \geqslant -2$	1	$f: x \geqslant -2$ but do not allow $x \geqslant -2$
	(b)	$[fg(2) =]f\left(\frac{12}{2^3 + 4}\right)[=f(1)]$ or $[fg(x) =]\left(\frac{12}{x^3 + 4}\right)^2 - 2$			M1 Evidence of correct first step eg $\frac{12}{2^3 + 4}$ or $g(2) = 1$ or $f(1)$ or $\left(\frac{12}{x^3 + 4}\right)^2 - 2$
			-1	2	A1 Must not come from any incorrect working
				II.	Total 3 marks
13	(a)		192	1	B1
	(b)	$3(c^2+2c) \text{ or } c(3c+6)$			M1
			3c(c+2)	2	A1 allow $(3c+0)(c+2)$ Do not IS
	1		1	II.	Total 3 marks

Question	Working	Answer	Mark	Notes			
14	(x-3)(3x+1)			M1 allow any one correct factorisation of numerator or			
	$\frac{4(x-3)(x+3)}{4(x-3)(x+3)}$			denominator $4(x^2-9)$ , $(2x+6)(2x-6)$ ,			
				(4x-12)(x+3), (x-3)(4x+12), 2(x-3)(2x+6)			
				2(2x-6)(x+3) oe or $(x-3)(3x+1)$ These may			
				appear on their own rather than as part of the fraction			
				M1 Both numerator and denominator factorised correctly.			
				These may appear on their own rather than as part of			
				the fraction.			
				The denominator does not need to have a common			
				factor but it must have a pair of correct brackets.			
				(not $4(x^2 - 9)$ ) but allow other factorisation.			
		3x+1	3	A1 Final answer – allow $4x + 12$ in the denominator. Do			
		4(x+3)		Not allow $2(2x+6)$			
·	Total 3 marks						

Que	stion		Working	Answer	Mark	Notes
15		Side/Angle	Reason			
		BQ = QC	Q is <b>midpoint/bisection</b> of $BC$			
		PQ = RC	AR = RC and $AR = PQ$ (opposite side of a			M1 Identifying a pair of equal sides/angles with a reason.
			parallelogram are equal)			They must state the pair of sides/angles and the reason
		QR = BP	AP = PB and $AP = RQ$ (opposite side of a			must include the words in bold.
			parallelogram are equal)			
		$\angle PBQ = \angle RQC$	Corresponding angles			
		$\angle BQP = \angle QCR$	Corresponding angles			M1 identifying a second relevant pair of equal sides/angles
		$\angle BPQ = \angle QRC$	$\angle BPQ = \angle PQR$ and $\angle PQR = \angle QRC$			with a reason. They must state the pair of sides/angles
			Alternate angles or			and the reason must include the words in bold.
			$\angle APQ = \angle ARQ$ & angle on a <b>straight line</b>			
				SSS or SAS or	3	A1 must state SSS, SAS, ASA or AAS and have all 3
				ASA or AAS		relevant sides/angles shown to be equal
				with the third		relevant sides/angles shown to be equal
				relevant angle		<b>NB</b> There may be alternative reasons. Look for at least 1
				or side shown to be equal.		correct mathematical word for each pair
				to be equal.		Total 3 marks
16	(a)			15	1	B1
	(b)	0.05 + 0.1 + (2x -	(0.1) + 0.2 + 0.3 + (3x + 0.2) = 1 oe	-		M1 Using $\sum p = 1$ . You may award the mark if this is
						seen in part (a) Award if they get $x = 0.05$ oe
						M1ft for subst their x into $3x + 0.2$ need to see working
						(or into $2x - 0.1$ and doing $1 - 0.65 -$ ("their $2x - 0.1$ "))
						to find the probability of 6. (x must be between 0 and
						0.27)
				0.35	3	A1 Allow 35%, $\frac{7}{20}$ oe
				0.33	3	$\frac{1}{20}$ Allow 3370, $\frac{1}{20}$ 0c
						Total 4 marks

Que	stion	Working	Answer	Mark	Notes			
17	(a)	$\frac{1}{2}(2)(6)\sin 30^{\circ}$ oe			M1			
			3	2	A1			
	(b)	$\cos x^{\circ} = \frac{4}{12} \text{ or } \sin x^{\circ} = \frac{[(\sin 90)]\sqrt{12^{2} - 4^{2}}}{12} \text{ or } $ $\tan x^{\circ} = \frac{\sqrt{12^{2} - 4^{2}}}{4} \text{ or } \cos x^{\circ} = \frac{12^{2} + 4^{2} - (\sqrt{12^{2} - 4^{2}})^{2}}{2 \times 12 \times 4}$			M1 Complete method (e.g. Pythagoras followed by sine, cosine rule, etc.) Allow $8\sqrt{2}$ or awrt 11.3 for $\sqrt{12^2 - 4^2}$			
			70.5	2	A1 awrt 70.5			
	Total 4 marks							

Ques	tion	Working	Answer	Mark	Notes
18					M1 One of $\frac{3}{9} \times \frac{2}{11}$ or $\frac{2}{9} \times \frac{4}{11}$
					or P(R, not R) ie $\frac{3}{9} \times \frac{9}{11}$ accept $\left(\frac{3}{9} \times \frac{4}{11} + \frac{3}{9} \times \frac{5}{11}\right)$
					or P( Y, not Y) ie $\frac{2}{9} \times \frac{7}{11}$ accept $(\frac{2}{9} \times \frac{2}{11} + \frac{2}{9} \times \frac{5}{11})$
					or P( G, not G) ie $\frac{4}{9} \times 1$ accept $\left(\frac{4}{9} \times \frac{2}{11} + \frac{4}{9} \times \frac{4}{11} + \frac{4}{9} \times \frac{5}{11}\right)$
					M1 Or two of $\frac{3}{9} \times \frac{9}{11}$ accept $\left(\frac{3}{9} \times \frac{4}{11} + \frac{3}{9} \times \frac{5}{11}\right)$
	$\left(\frac{3}{9} \times \frac{2}{11}\right) + \left(\frac{2}{9} \times \frac{2}{11}\right)$	$\left(\frac{1}{1}\right)$			or $\frac{2}{9} \times \frac{7}{11}$ accept $\left(\frac{2}{9} \times \frac{2}{11} + \frac{2}{9} \times \frac{5}{11}\right)$
					or $\frac{4}{9} \times 1$ accept $\left(\frac{4}{9} \times \frac{2}{11} + \frac{4}{9} \times \frac{4}{11} + \frac{4}{9} \times \frac{5}{11}\right)$
	$1 - \left( \left( \frac{3}{9} \times \frac{2}{11} \right) + \left( \frac{2}{9} \right) \right)$	$\times \frac{4}{11}$			M1dep on both previous method marks being awarded. Attempt at correct calculation (oe)
			85 99	4	A1 oe awrt 0.86 awrt 85%
					Total 4 marks
19	UB of 1.32 is 1.32	5			B1 1.325 seen implied by correct answer
	LB of 9.8 is 9.75				B1 9.75 seen implied by correct answer
	$6.28\sqrt{\frac{1.325}{9.75}}$				M1 Subst in their $L > 1.32$ and $g < 9.8$
			2.32	4	A1 awrt 2.32
					Total 4 marks
20	fd = 1.6, 0.5, 1.4,	0.6, 0.2			M1 for use of area to work out freq density. Implied by the

Questio	n Working	Answer	Mark	Notes
				frequency of 30 – 45 being 9 or a bar drawn at the correct height
		7, 9 Heights at 0.5 and 0.2	4	A3 for all four correct, A2 for three and A1 for two The heights must be drawn on the histogram and be for 10 - 20 10 small squares high, for 45 - 60 4 small square high
				Total 4 marks
21	x(3w-2y)-15(3w-2y) = 3(x+2y) or			M1 Multiply through by $(3w-2y)$ and $3$ – not necessarily
	(3w-2y)(x-15)=3(x+2y)			at the same time
	3x + 2xy - 3xw = 24y - 45w			M1 Collect <i>x</i> terms on one side and other terms on the opposite side (indep of first M)
	x(3+2y-3w) = 24y-45w			M1 taking <i>x</i> out as a common factor of an equation correctly
		$x = \frac{24y - 45w}{3 + 2y - 3w}$	4	A1 Final answer – or equivalent – but must a single fraction. The numerator and denominator need not be simplified. Do not ISW
,			•	Total 4 marks
22	$BF = \sqrt{0.5^2 + 1.2^2}  [\Rightarrow BF = 1.3]$			M1 Award for $\sqrt{0.5^2 + 1.2^2}$ or 1.3 or correct method using trig to find an angle and then to find FB
	[Area of triangle <i>ABF</i> (or <i>CDE</i> )] = $0.5 \times 0.5 \times 1.2$ [=0.3] or [area of <i>ABF</i> + <i>DCE</i> =] $2 \times 0.5 \times 0.5 \times 1.2$ [=0.6]			M1 Allow use of $\frac{1}{2}ab\sin c$ with a correct method used to find the angle
	[Area of rectangle $ADEF$ ] = $0.5 \times 2.3$ [=1.15] <b>and</b> [Area of rectangle $ABCD$ ] = $1.2 \times 2.3$ [=2.76]			M1
	[Area of rectangle $BCEF$ ]= $2.3 \times "1.3"$ [=2.99]			M1 dep on 1 <sup>st</sup> M1 being awarded – allow their 1.3
		7.5	5	A1 cao
				Total 5 marks

Question	Working	Answer	Mark	Notes
23 (a)	8 6 17 3 2 11		3	B3 for all 8 correct B2 for 6 or 7 correct B1 for 4 or 5 correct  If all other numbers are correct allow a blank for zero. Allow if written as a sum eg $18 - 2 - 13$ Do not allow entries in terms of a letter eg $x$
(b)		14	1	B1ft Allow ft for "their 8"+"their 6" but do not award ft if one of the required areas is a blank or if in terms of x
(c)		22	1	B1ft Allow ft for "their 17"+"their 2"+"their 3" but do not award ft if one of the required areas is a blank
				Total 5 marks

Ques	etion	Working	Answer	Mark	Notes
			Allowel	IVIAIK	INOTES
24	(a)	$\overrightarrow{YX} = \overrightarrow{YO} + \overrightarrow{OX}$ or $\overrightarrow{YX} = \overrightarrow{OX} - \overrightarrow{OY}$ or $3\mathbf{a} - 5\mathbf{b} + 2\mathbf{a} + 3\mathbf{b}$			M1do not accept $\overrightarrow{XY}$
			5a-2b	2	A1 oe
	(b)	$\left[\overrightarrow{YZ} = \overrightarrow{OZ} - \overrightarrow{OY} = \right] \left(-\frac{2}{9}\mathbf{a} + \frac{35}{9}\mathbf{b}\right) - \left(-3\mathbf{a} + 5\mathbf{b}\right)$			M1 any 1 correct method. ft their $\overrightarrow{YX}$ from part a. and their KZ in the $4/5^{th}$ line. May be implied by one of
		$\left[ \overrightarrow{ZX} = \overrightarrow{ZO} + \overrightarrow{OX} = \right] - \left( -\frac{2}{9}\mathbf{a} + \frac{35}{9}\mathbf{b} \right) + 2\mathbf{a} + 3\mathbf{b}$			$\overrightarrow{YZ} = \frac{25}{9}\mathbf{a} - \frac{10}{9}\mathbf{b}$
		$\left[\overrightarrow{ZX} = \overrightarrow{YX} - \overrightarrow{YZ} = \right] ("5\mathbf{a} - 2\mathbf{b}") - \left(\frac{25}{9}\mathbf{a} - \frac{10}{9}\mathbf{b}\right)$			$\overrightarrow{ZX} = \frac{20}{9}\mathbf{a} - \frac{8}{9}\mathbf{b}$
		$\left("5\mathbf{a} - 2\mathbf{b}"\right) = k\left("\frac{20}{9}\mathbf{a} - \frac{8}{9}\mathbf{b}"\right)$			$k = \frac{4}{9}$
		$j("5\mathbf{a} - 2\mathbf{b}") = \left("\frac{20}{9}\mathbf{a} - \frac{8}{9}\mathbf{b}"\right)$			$j = \frac{9}{4}$
		$\overrightarrow{YZ} = \frac{25}{9}\mathbf{a} - \frac{10}{9}\mathbf{b} \text{ and } \overrightarrow{ZX} = \frac{20}{9}\mathbf{a} - \frac{8}{9}\mathbf{b}$			A1 accept decimals for fractions if meaning clear
		or $k = \frac{4}{9}$ or $j = \frac{9}{4}$			
			5:4	3	A1 Allow $\frac{5}{4}$ :1 or 1: $\frac{4}{5}$ or 1.25:1 or 1:0.8 do not
					allow $\frac{4}{5}\overrightarrow{YX} = \overrightarrow{ZX}$ oe
					Total 5 marks

Ouc	stion	Working	Answer	Mark	Notes
		vvorking		IVIAIK	
25	(a)		54		B1
		eg The sum of the <b>opposite</b> angles in a <b>cyclic</b> quadrilateral is $180^{\circ}$	Reason	2	B1 need bold – other reasons may be given - must be associated with method used (see below for bold words)
	(b)	$\angle BOD = 108^{\circ}$			M1
		360 – (108 + 126 + 62)			M1ft their 108 but must be clear it is BOD
			64		A1
		Angle at centre of a circle is twice angle at the circumference or angles in a quadrilateral add up to 360° or angles at a point add up to 360°	Reason	4	B1 need one reason only and bold words – must be associated with method used
		Alternative method marks 1 $\angle BCO = 62^{\circ}$			M1
		$\angle OCD = 126 - 62$			M1ft their 62 but must be clear it is BCO
			64		A1
		Base(oe) angles of an isosceles triangle are the same			B1 need bold words – must be associated with method used
		Alternative method marks 2 Let $\angle ODA = y :: \angle ABO = "54" + y$			M1ft Using their part (a)
		$\angle CDA = 360 - 126 - 62 - "54" - ("54" + y)$			M1
			64		A1
		<b>Isosceles</b> triangle, angles in a <b>triangle</b> add up to <b>180</b> ° and angles in a <b>quadrilateral</b> add up to <b>360</b> °	Reason		B1 need one reason only and bold words – must be associated with method used
					Total 6 marks

Question	Working	Answer	Mark	Notes
26	$\mathbf{A}^2 = \begin{pmatrix} -11 & 9 \\ -15 & -14 \end{pmatrix}$			M1Condone one error
	$\mathbf{AB} = \begin{pmatrix} 11 & 2k - 3 \\ -19 & -5k - 1 \end{pmatrix}$			M1 Condone one error
	$\mathbf{A}^2 - \mathbf{A}\mathbf{B} = \begin{pmatrix} -22 & 12 - 2k \\ 4 & 5k - 13 \end{pmatrix}$			A1 cao
	$\det(\mathbf{A}^2 - \mathbf{A}\mathbf{B}) = -22(5k - 13) - 4(12 - 2k)$			M1 ft their $\mathbf{A}^2 - \mathbf{AB}$
	$-22(5k-13)-4(12-2k) = 3k+28 \implies k = \dots$			M1dep on previous M1- Sets their determinant equal to $3k + 28$ and attempts to solve for $k$
		k=2	6	A1
			1	Total 6 marks
27	Area of large semicircle = $\frac{1}{2}\pi x^2$ or half large semicircle = $\frac{1}{4}\pi x^2$			M1
	Area of small circle = $\pi \left(\frac{x}{2}\right)^2$ or half small circle = $\frac{1}{2}\pi \left(\frac{x}{2}\right)^2$			M1
	Shaded region = $\frac{1}{2} \left( \frac{1}{2} \pi x^2 - \pi \left( \frac{x}{2} \right)^2 \right) \left[ = \frac{1}{8} \pi x^2 \right]$			A1
	Perimeter = $x + \frac{1}{4}(2\pi x) + \frac{1}{2}\left(2\pi\left(\frac{x}{2}\right)\right)\left[=\pi x + x\right]$			M1 dep on first two methods.
	$"\frac{\pi x^2}{8}" = "\pi x + x"$			M1 Equates their expressions for the perimeter and area of shaded region
		$x = \frac{8(\pi + 1)}{\pi}$	6	A1 Or equivalent
·				Total 6 marks

Question		Working	Answer	Mark	Notes	
28	(a)	$\left[v=\right]-9t^2+12t+k$			M1 A three term expression is needed with 1 correct term or a 4 term expression with 2 terms correct	
		$-9(2)^2 + 12(2) + k = 9$			M1dep Substituting $t = 2$ into their equation and equating to 9 Allow substitution of 21 and showing it equals 9	
			k = 21	3	A1 stating $k = 21$ following a fully correct solution with no errors. Note that answer given in question	
28	(b)	$-9t^2 + 12t + 21 = 0$			M1	
		eg $(3t-7)(t+1)=0$			M1 Solving their trinomial quadratic.  For factorising any 3 term quadratic which when expanded, the result gives at least 2 of the 3 terms from their trinomial.  correct use of formula by substituting values in correctly or completing the square. Allow one slip.	
			$\frac{7}{3}$	3	A1 oe awrt 2.3 with negative value rejected	
28	(c)	$OA = -3("7/3")^{3} + 6("7/3")^{2} + 21("7/3") + 4$			M1ft Substitute their positive $t$ from part (b) into expression for $x$	
			48	2	A1 cao do not ISW	
	Total 8 marks					

Pearson Education Limited. Registered company number 872828 with its registered office at 80 Strand, London, WC2R 0RL, United Kingdom