

## Mark Scheme (Results)

January 2012

International GCSE Mathematics (4MA0) Paper 4H



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Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.

Question	Working	Answer	Mark	Notes
1.	$\frac{4.2}{1.12}$		2	M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$
		3.75		A1
				Total 2 marks

2.	135		3	M1
	180			
	0.75 oe			A1
		45		A1 cao
				Total 3 marks

3.	4x = 7  or  4x = 2 + 5 or $7x - 3x = 7 \text{ oe}$ or $4x - 7 = 0 \text{ oe}$		3	M2	for correct rearrangement with x terms on one side and numbers on the other AND collection of terms on at least one side or for $4x - 7 = 0$ oe M1 for $7x - 3x = 2 + 5$ oe ie correct rearrangement with x terms on one side and numbers on the other
		$1\frac{3}{4}$ oe		A1	Award full marks for a correct answer if at least 1 method mark scored
					Total 3 marks

 1 7 7		5	B2 for 1 7 7 in any orde B1 for three positive w numbers with either a	hole
			or a sum of 15 SC Award B1 for 0 7	
	6		B1 cao	
			Тс	otal 3 marks

5.	One correct point plotted or stated		4	<b>B</b> 1	May appear in table
	2nd correct point plotted or stated			B1	May appear in table
	Correct line between $x = -2$ and $x = 4$			B2	B1 for a line joining two correct, plotted points
					Total 4 marks

<b>6.</b> (a)	1 + 7 or 8		2	M1	8 may be denominator of fraction or coefficient in an equation such as 8x = 32	<i>SC</i> If M0 A0, award B1 for 4 : 28
		28		A1	cao	
(b)	32 × 45 or 1440 or 14.4(0)m		3	M1		
	"1440"			M1	dep	
	72					
		20		A1	cao	
					Tot	tal 5 marks

7.	Fully correct factor tree or repeated division		3	M2 M1 for factor tree or repeated
	or 2, 2, 2, 5, 5 or $2 \times 2 \times 2 \times 5 \times 5$			division with 2 and 5 as factors
		$2^3 \times 5^2$		A1 Also accept $2^3.5^2$
				Total 3 marks

8.	$y^{3+n-1} = y^{6} \text{ oe or } y^{3+n} = y^{7} \text{ oe}$ or $3+n-1 = 6$ oe or $y^{n} = \frac{y^{7}}{y^{3}}$ or $y^{n} = \frac{y^{6}}{y^{2}}$ or $y^{n} = y^{4}$		2	M1	<i>SC</i> if M0, award B1 for an answer of $y^4$
		4		A1 cao	
					Total 2 marks

<b>9.</b> (a)	Complete, correct expression which, if correctly evaluated, gives 48 eg $4 \times \frac{1}{2} \times 6 \times 4$ , $2 \times \frac{1}{2} \times 12 \times 4$ , $\frac{1}{2} \times 12 \times 8$		3	M2 M1 for correct expression for area of one relevant triangle $eg \frac{1}{2} \times 6 \times 4, \frac{1}{2} \times 6 \times 4 \sin 90^{\circ},$ $\frac{1}{2} \times 8 \times 6, \frac{1}{2} \times 12 \times 4$
		48		A1 cao
(b)	$4^2 + 6^2 = 16 + 36 = 52$		3	M1 for squaring and adding
	$\sqrt{4^2 + 6^2}$			M1 (dep) for square root
		7.21		A1 for answer which rounds to 7.21 (7.211102)
				Total 6 marks

<b>10.</b> (i)	$-1\frac{1}{2} < x \le 2$	4	B2 Also accept $-\frac{3}{2} < x \le 2$ or answer
			expressed as two separate inequalities
			B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$
			or $x \le 2$ (these may be as part of a
			double-ended inequality)
			or $-\frac{6}{4} < x \le \frac{8}{4}$
(ii)	-1 0 1 2		B2 B1 for 4 correct and 1 wrong
			or for 3 correct and 0 wrong
			Total 4 marks

PMT

<b>11.</b> (a)	$75 = 3 \times 5^{2} \text{ and } 90 = 2 \times 3^{2} \times 5$ or 1,3,5,15,25,75 and 1,2,3,5,6,9,10,15,18,30,45,90 or 3 \times 5	15	2	M1	Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 Prime factors may be shown as factor trees or repeated division
(b)	$2 \times 3^{2} \times 5^{2} \text{ oe eg } 6 \times 3 \times 5^{2}$ or 75,150,225,300,375,450 and 90,180,270,360,450		2	M1	Also award for $\frac{75 \times 90}{15}$
		450		A1	Total 4 marks

12.	(a)	Rotation	3	B1			
		90°		B1	Also accept quarter turn or -270° (B0 for 90° clockwise)	These marks are independent but award no marks the answer is not a single	
		(0, 0)		B1	Also accept origin, O	transformation	
	(b)	<b>R</b> correct	1	<b>B</b> 1			
	(c)	Rotation 90°	2	B1	Accept quarter t -270° instead o		As for (a)
		(3, 1)		B1	ft from their <b>R</b> if it is a translation of the correct <b>R</b>		
						Tot	al 6 marks

<b>13.</b> (a)	4y = 10 - 3x or $-4y = 3x - 10$		3 N	11 May be implied by second M1 or
				by $y = -\frac{3}{4}x + c$ even if value of c is incorrect. or finds coordinates of 2 points on
				the line eg (0, 2.5), $x = 2$ , $y = 1$ , table, diagram.
	$y = \frac{5}{2} - \frac{3}{4}x \text{ oe or } y = \frac{10}{4} - \frac{3}{4}x \text{ oe}$ or $y = \frac{10 - 3x}{4}$ oe		Ν	A1 or for clear attempt to evaluate $\frac{\text{vert diff}}{\text{horiz diff}}$ for their pts
		$-\frac{3}{4}$	1	Award 3 marks for correct answer if either first M1scored or no working shown. SC If M0, award B1 for $-\frac{3}{4}x$

<b>13</b> (b)	eg $9x + 12y = 30$ 10x - 12y = 46	eg $15x + 20y = 50$ 15x - 18y = 69		5	M1	for coefficients of <i>x</i> or <i>y</i> the same or for correct rearrangement of one equation followed by correct substitution in the other eg $5x - 6\left(\frac{10 - 3x}{4}\right) = 23$
	<i>x</i> = 4	$y = -\frac{1}{2}$			A1	cao dep on M1
					M1	(dep on 1st M1) for substituting for other variable
			$x = 4,  y = -\frac{1}{2}$		A1	Award 4 marks for correct values if at least first M1 scored
			$(4, -\frac{1}{2})$		B1	Award 5 marks for correct answer if at least first M1 scored ft from their values of <i>x</i> and <i>y</i>
						Total 8 marks

14.	(a)	55 11.	5 155 177 190 200	1	B1	cao
	(b)		Points correct	2	B1	$\pm \frac{1}{2}$ sq ft from sensible table ie
						clear attempt to add frequencies
			Curve		B1	ft from points if 4 or 5 correct
			or			or ft correctly from sensible table
			line segments			or if points are plotted consistently
						within each interval at the correct
						heights
						Accept curve which is not joined
						to the origin
	(c)	26 indicated on cf graph		2	M1	for 26 indicated on cf graph
						– accept 26-27 inc
			approx 60 from		A1	If M1 scored, ft from cf graph
			correct graph			If M1 not scored, ft only from
						correct curve & if answer is
						correct ( $\pm \frac{1}{2}$ sq tolerance) award
						M1 A1
						Total 5 marks

15.	-4 < x < 4	2	B2 B1 for $x < 4$ or $x > -4$ or $x < \pm 4$
			or $x < \sqrt{16}$
			SC B1 for $-4 \le x \le 4$
			Total 2 marks

16.	(a)	$\frac{3}{8} + \frac{2}{8}$ oe		2	M1
			$\frac{5}{8}$		A1
	(b)(i)	$\frac{2}{8} \times \frac{1}{7}$ appearing once only		5	M1 Sample space method –
			$\frac{2}{56}$ or $\frac{1}{28}$		A1 for $\frac{2}{56}$ or $\frac{1}{28}$ award 2 marks for correct or for 0.036 or for answer rounding to 0.036
	(ii)	$\frac{2}{8} \times \frac{3}{7} + \frac{3}{8} \times \frac{2}{7}$ or $2 \times \frac{2}{8} \times \frac{3}{7}$ oe			M1for one correct productM1for completely correct expression
			$\frac{12}{56}$		A1 for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21
					Note for (b)(ii): sample space method – award 3 marks for correct answer; otherwise no marks $SC M1 \text{ for } \frac{2}{8} \times \frac{3}{8} \text{ or } \frac{3}{8} \times \frac{2}{8}$ M1 (dep) for $\frac{2}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{2}{8} \text{ oe}$ SC  Sample space method – award 2 marks for $\frac{12}{64}$ oe; otherwise no marks
					Total 7 marks

17.	(a)		2	1	B1	cao
	(b)		<i>x</i> < 6	2	B2	cao B1 for eg $x \le 6$
						or2, -1, 0, 1, 2, 3, 4, 5
						SC B1 for $x \ge 6$
	(c)		7	1	B1	cao
	(d)	g(0) = 15		2	M1	for 15 seen
			3		A1	cao If M0, award B1 for $\pm 3$ oe
	(e)	<i>k</i> = 12		3	M1	May be stated or indicated on diagram. May be implied by one correct solution.
			-0.7 or -0.8 3.8		A2	A1 for solution rounding to -0.7 or -0.8 A1 for solution rounding to 3.8
	(f)	tan drawn at $x = 3.5$		3	M1	tan or tan produced passes between points $(3, 3 \le y \le 6)$ and $(4, 11 \le y \le 14)$
		vertical difference horizontal difference			M1	finds their $\frac{\text{vertical difference}}{\text{horizontal difference}}$ for two points on tan or finds their $\frac{\text{vertical difference}}{\text{horizontal difference}}$ for two points on curve, where one of the points has an <i>x</i> -coordinate between 3 and 3.5 inc and the other point has an <i>x</i> -coordinate between 3.5 and 4 inc
			6.5 – 11 inc		A1	dep on both M marks
						Total 12 marks

18.	$(\cos x^{\circ} =) \frac{4^{2} + 6^{2} - 8^{2}}{2 \times 4 \times 6}$ or $8^{2} = 4^{2} + 6^{2} - 2 \times 4 \times 6 \cos x^{\circ}$		3	M1 for correct substitution in Cosine Rule
	$(\cos x^{\circ} =) -0.25$ oe			A1
		104.5		A1 for value rounding to 104.5 (104.4775)
				Total 3 marks

<b>19.</b> (a)	æ 7			B2	for all correct B1 for 2 or 3 correct
(b)(i)		10	2	<b>B</b> 1	cao
(ii)		25		<b>B</b> 1	cao
					Total 4 marks

20.	$\pi \times r \times 9 = 100$ oe	5	5 M1	
	( <i>r</i> =) 3.53677		A1	for 3.53 or for value rounding to 3.54 $(3.14 \rightarrow 3.53857)$
	$\sqrt{9^2 - "3.53"^2}$		M1	
	( <i>h</i> =) 8.2759		A1	for 8.27 or for value rounding to 8.28
		108	A1	
				Total 5 marks

21.	(a)		8y <sup>6</sup>	2	B2 B1 for 8 B1 for $y^6$
	(b)	$2^{p} \times (2^{3})^{q} = 2^{p} \times 2^{3q} = 2^{p+3q}$	p + 3q	2	B2 B1 for $2^{3q}$ seen
					Total 4 marks

<b>22.</b> (a)(i)		3 <b>a</b> + 3 <b>b</b> oe	3	B1
(ii)		2 <b>a</b> + 2 <b>b</b> oe		B1 Accept eg $\frac{2}{3}(3\mathbf{a}+3\mathbf{b})$
(iii)		<b>a</b> + 2 <b>b</b> oe		B1 Accept eg $2\mathbf{a} + 2\mathbf{b} - \mathbf{a}$
(b)	$\overrightarrow{DF} = 2\mathbf{a} + 4\mathbf{b}$ oe		2	M1 Also award for $\overrightarrow{EF} = \mathbf{a} + 2\mathbf{b}$ oe
		$ \overrightarrow{DF} = 2 DE \text{ oe} $ $ \overrightarrow{PF} = 2 DE = \overrightarrow{EF} $		A1 Also award A1 for an acceptable explanation in words.
				Total 5 marks

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